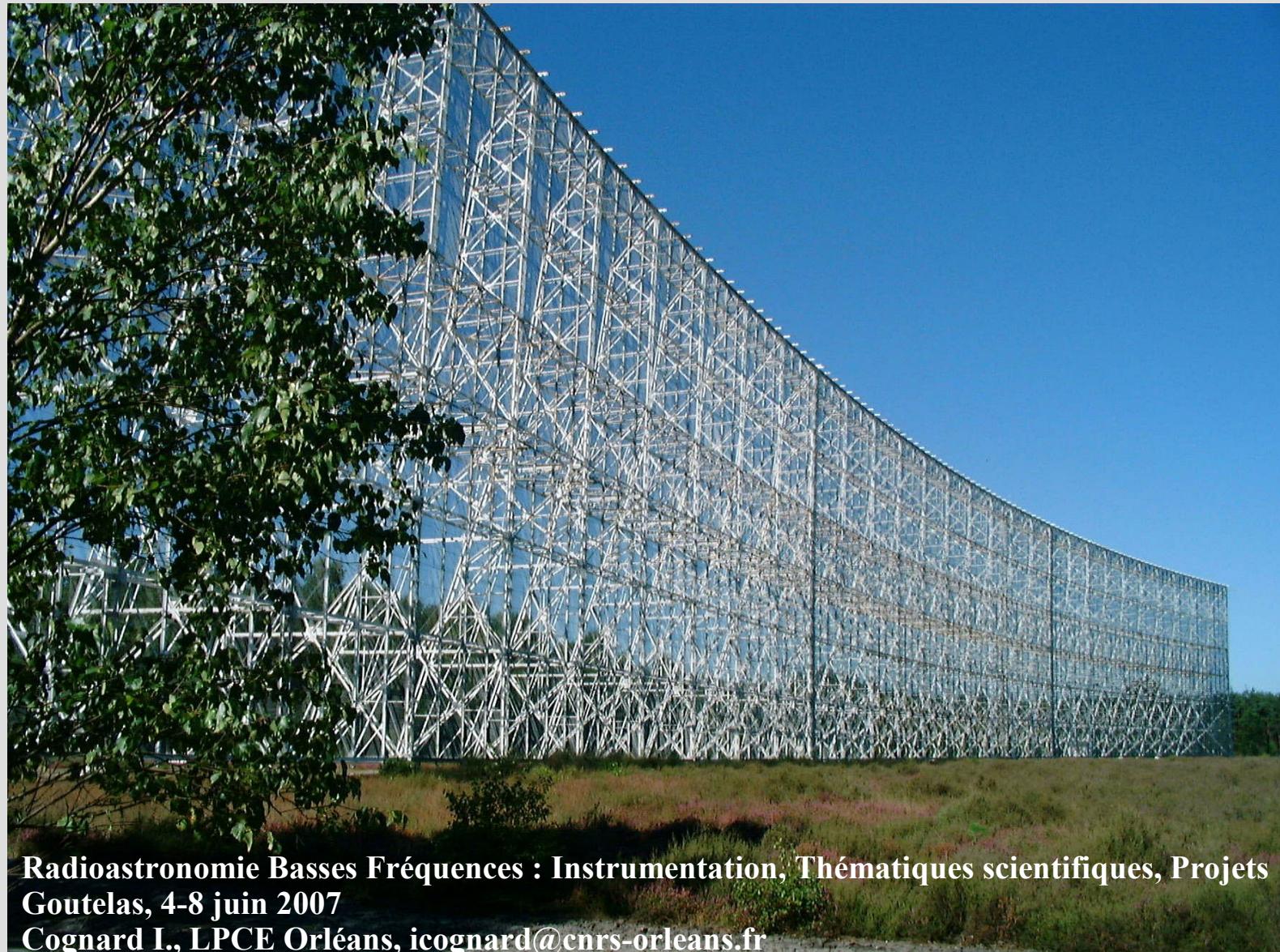


De la métrologie en radioastronomie

Metrology in radioastronomy



Radioastronomie Basses Fréquences : Instrumentation, Thématisques scientifiques, Projets
Goutelas, 4-8 juin 2007
Cognard I., LPCE Orléans, icognard@cnrs-orleans.fr

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- Stellar evolution

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- Scattering

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CP 1919



August 1967
Cambridge, UK
Jocelyn Bell

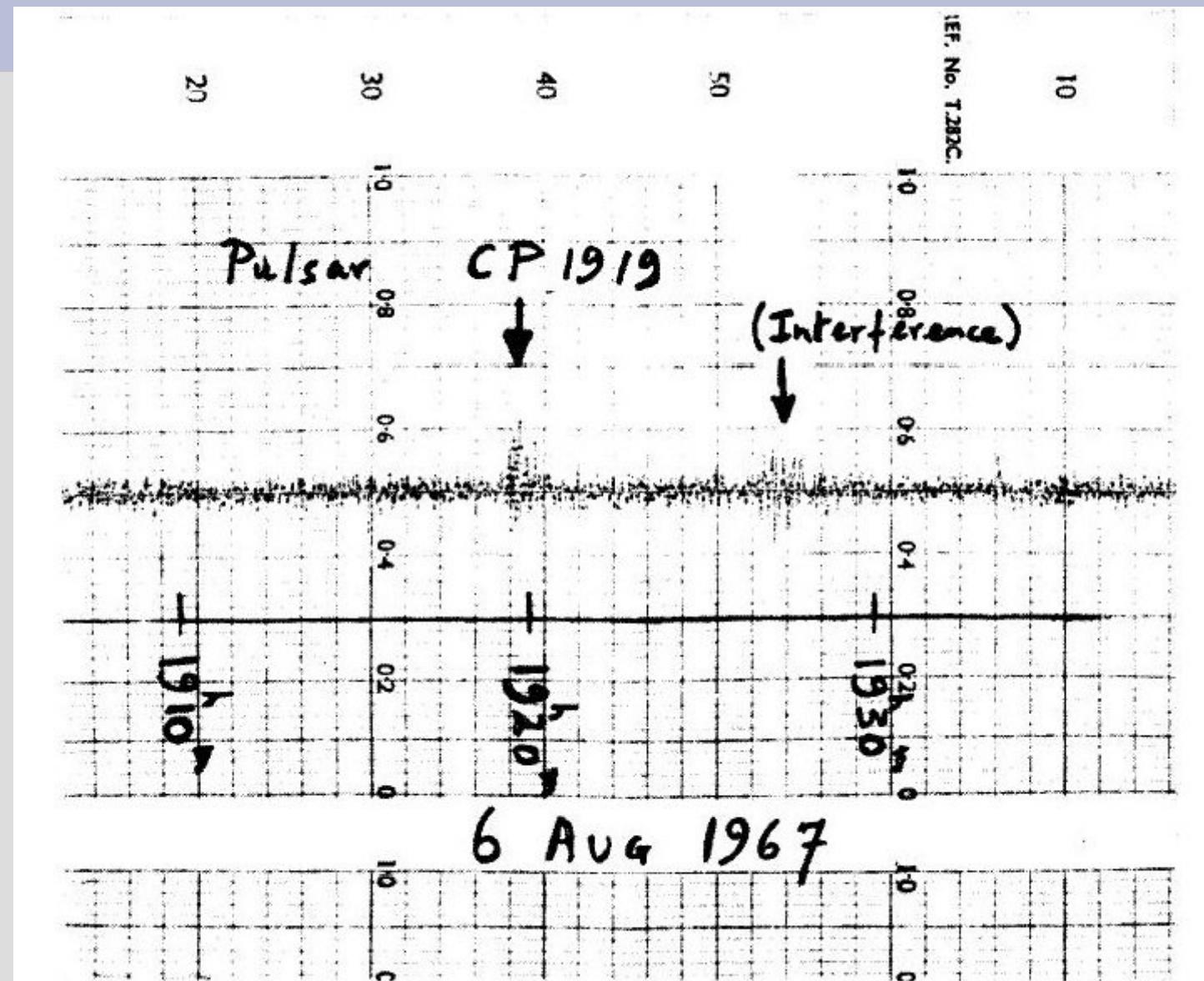
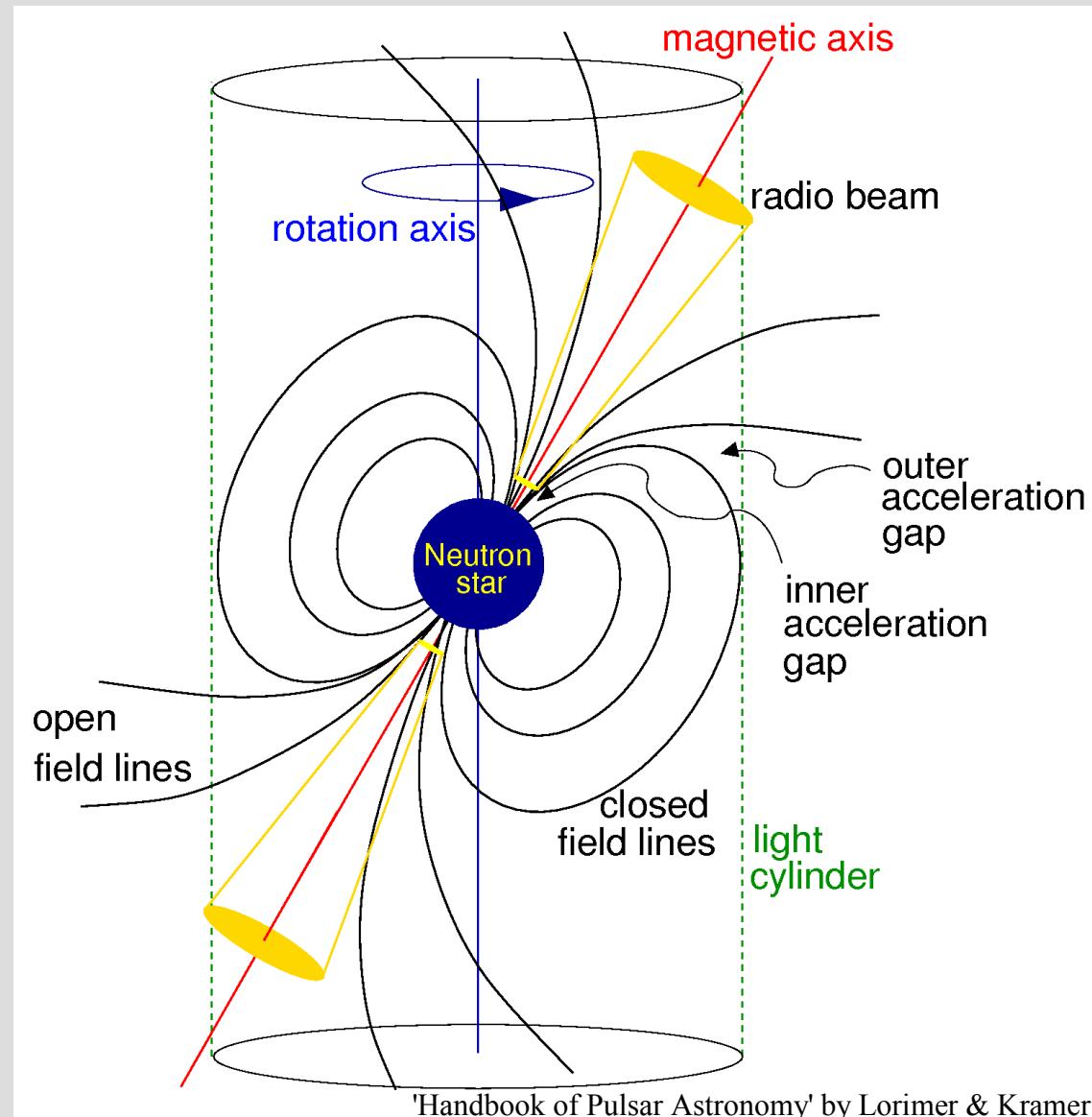


Fig. 1. The first signals from CP 1919.

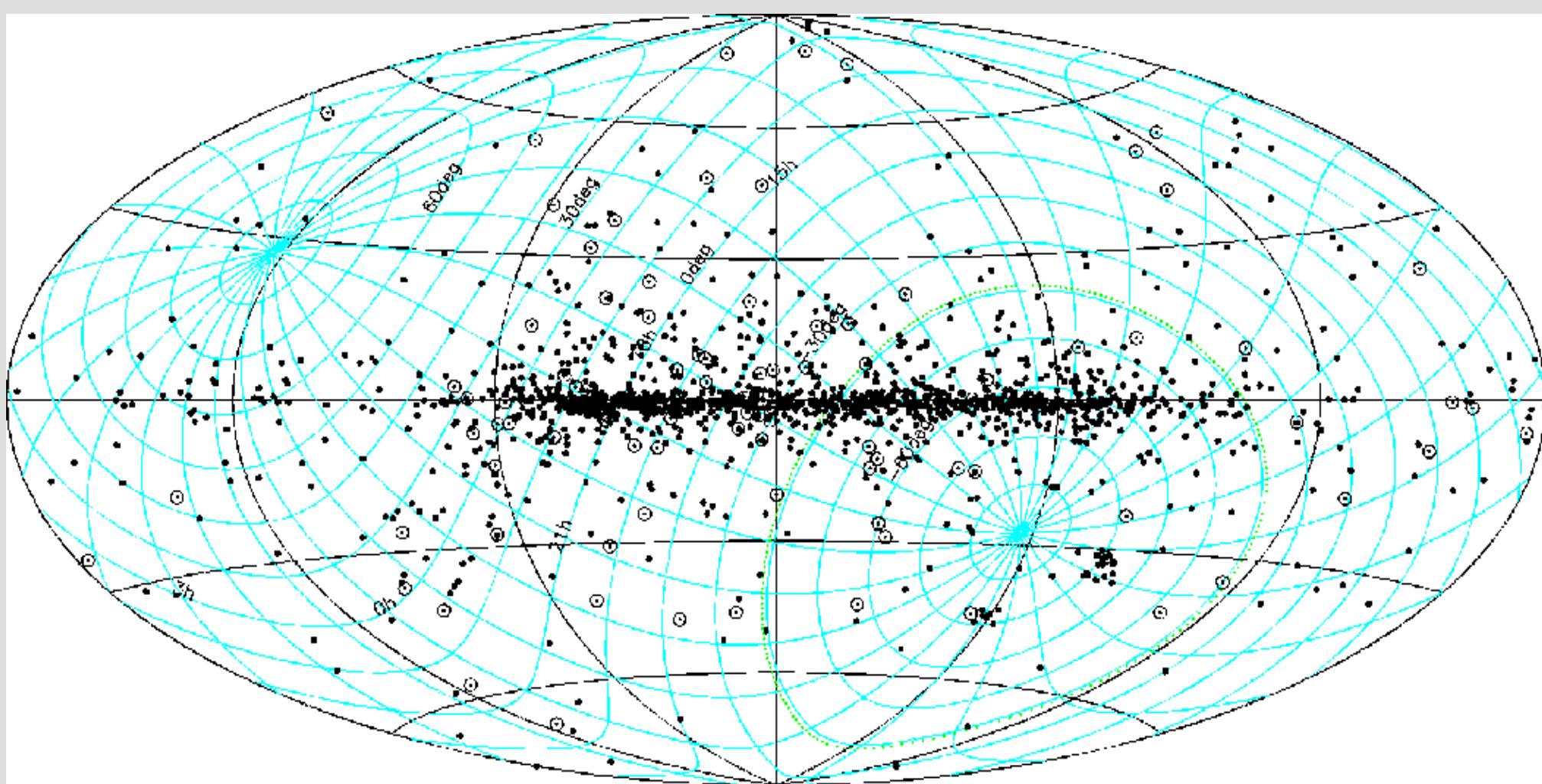
a pulsar is a highly magnetized neutron star

massive star
→ supernovae
→ neutron star

a neutron star +
a magnetic field
→ a pulsar



Pulsars in the Galaxy

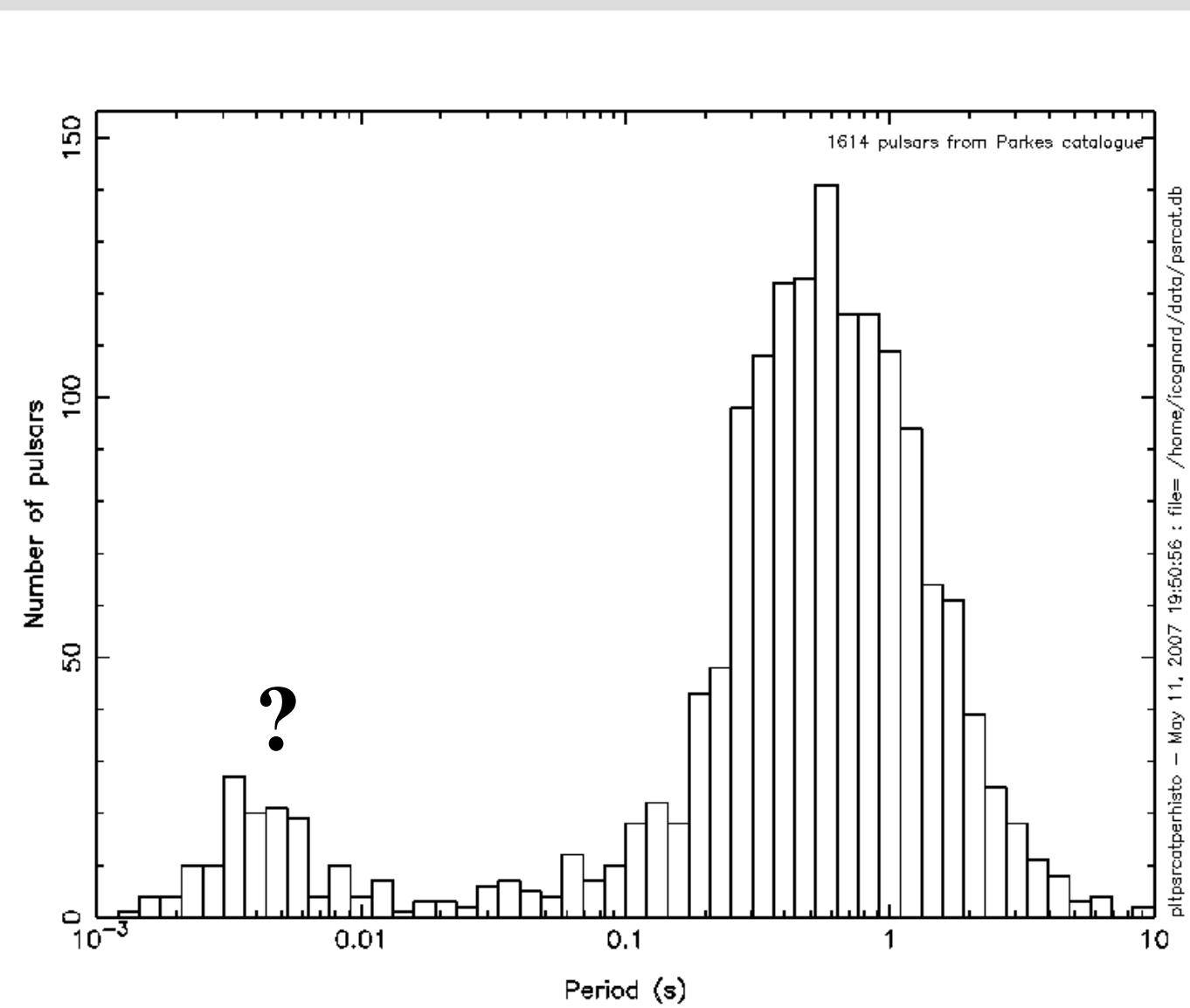


1614 pulsars

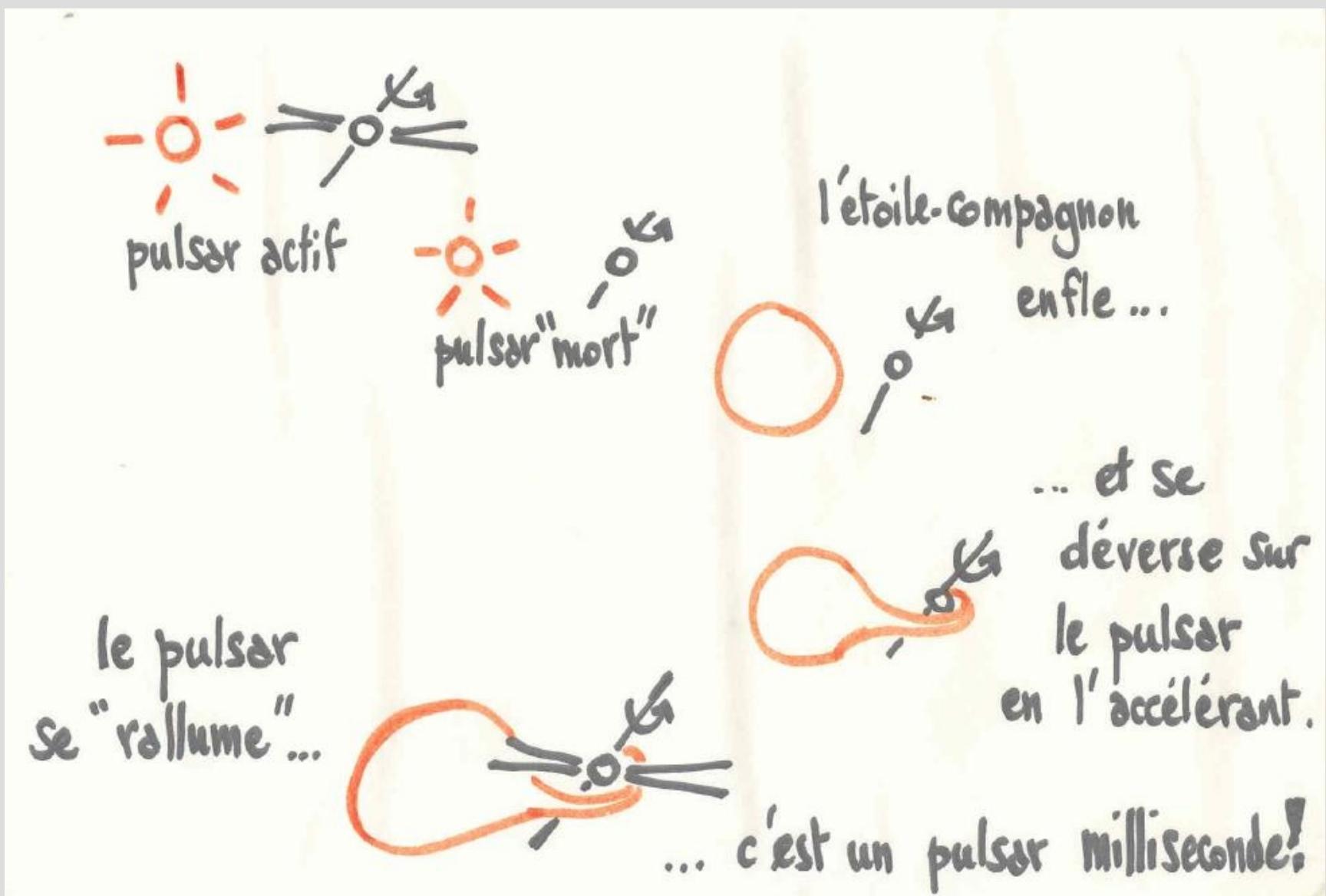
<http://www.atnf.csiro.au/research/pulsar/psrcat/>

Period distribution of pulsars

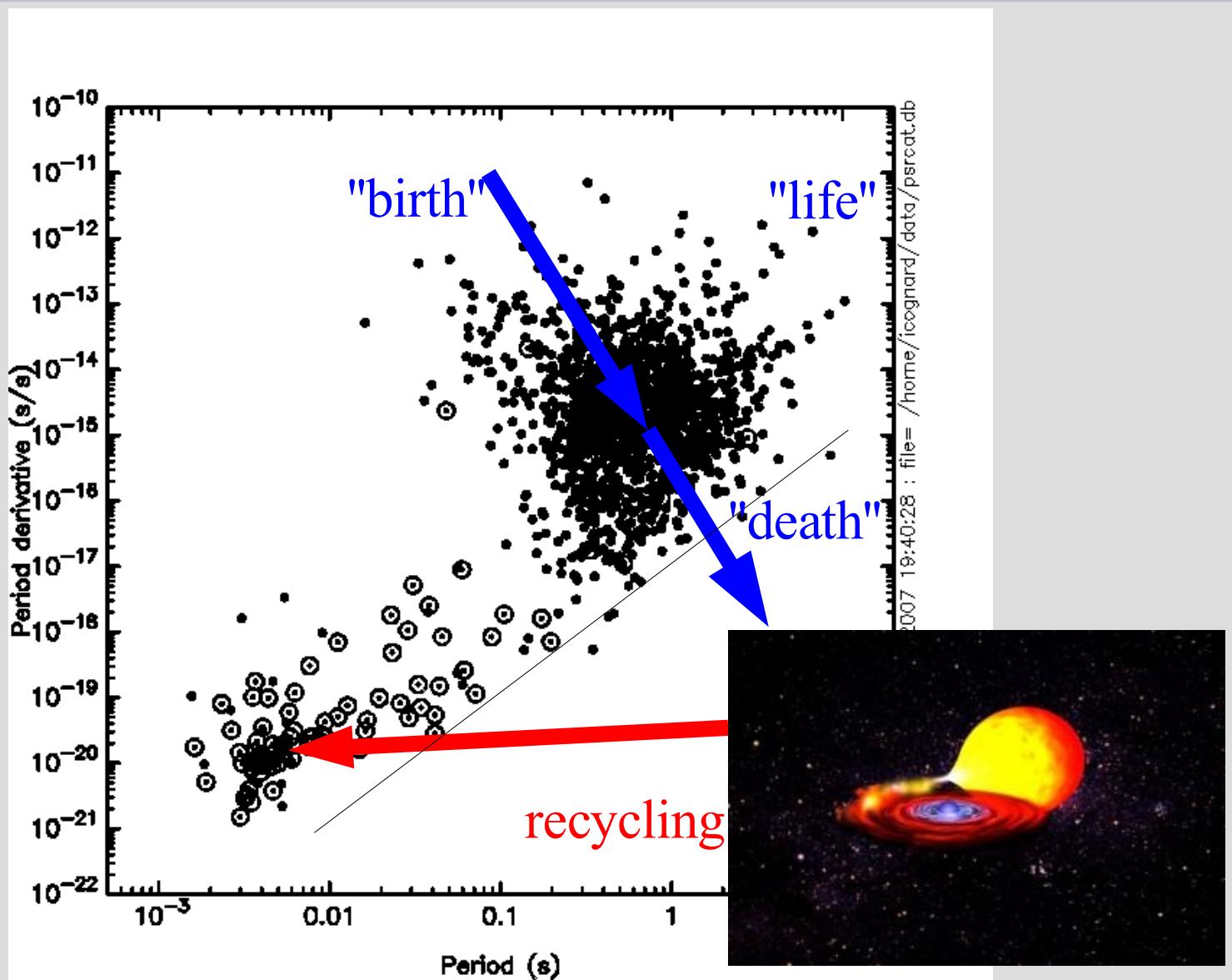
Periods of radio pulsars spans from 1.5ms to 8.5sec



Recycling...



Period - Period derivative diagram (or "Hertzsprung-Russell" diagram for pulsars)



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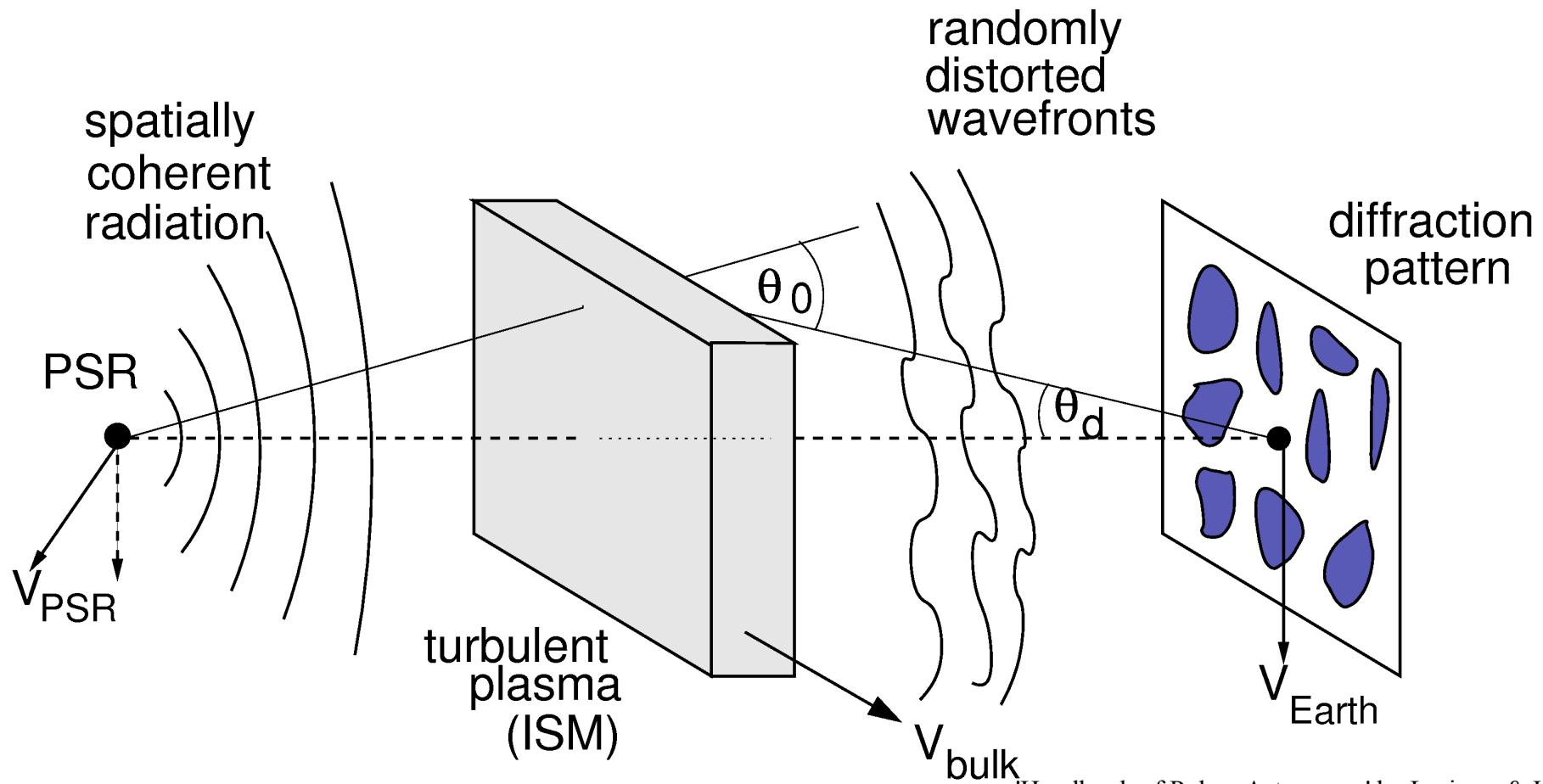
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Scattering régimes

an assumption...

the turbulent medium is a **thin phase changing screen**



Fresnel scale

$\varphi(x, y)$ is the phase change introduced by the screen
at transverse position (x,y)

the amplitude received at position (X,Y) on the observer plane
is given by the **Fresnel-Kichhoff integral** (Born & Wolf, 1980)

$$\Psi(X, Y) = \frac{e^{-i\pi/2}}{2\pi r_F^2} \iint \exp[i\varphi(x, y) + i\frac{(x-X)^2 + (y-Y)^2}{2r_F^2}] dx dy$$

where r_F is the Fresnel scale, $r_F = \sqrt{\lambda D / 2\pi}$

region inside r_F contributes coherently to the integral,
while outside regions cancel because of rapid oscillations

Diffractive length scale

turbulent medium : random phase fluctuations $D_\varphi(x, y)$
described by the 'phase structure function'

$$D_\varphi(x, y) = \langle [\varphi(x' + x, y' + y) - \varphi(x', y')]^2 \rangle_{x', y'}$$

i.e. the mean square phase difference between 2 points separated by (x,y)

if Kolmogorov turbulence,

isotropic and large outer scale and small inner scale

$$D_\varphi(r) = (r/r_{diff})^{5/3}, \quad r^2 = x^2 + y^2$$

r_{diff} is the diffractive length scale

the transverse separation for which the r.m.s. phase difference is 1 rad

... the Fried length, r_o , in optical astronomy

Scattering régimes

$r_{diff} \gg r_F$ **weak scattering**

random phase fluctuations within the first Fresnel zone are small

$r_{diff} \ll r_F$ **strong scattering**

then $D_\varphi(r_F) \gg 1$, r_F is no longer relevant
and r_{diff} is now the characteristic size of a coherent patch

For the observer in (X, Y) ,
there will be many points (x, y) on the scattering screen
with stationary phase...
that is **multipath propagation**

Scattering media in astronomy

	medium	wavelength	weak scattering	strong scatterring
optical	Earth's atmosphere	0.5μ	mostly	near horizon
radio	troposphere	20cm	yes	no
	ionosphere	3m	yes	sometimes
	solar wind	1m	mostly	close to the Sun
	interstellar medium	1m	no	yes

Strong scattering

the spectrum of flux variations has two peaks at widely separated length scales

diffractive scintillation

a dominant peak corresponding to flux variations on lengthscales $\sim r_{\text{diff}}$

a large number of coherent patches scatters radiation into a diffraction cone of angle $\Theta_{\text{scatt}} \sim r_{\text{ref}}/D$, interfering together

random interference pattern

very strict limit on the angular size :

virtually only pulsars show diffractive scintillation

refractive scintillation

a second peak corresponding to weak flux variations

on much longer lengthscales $\sim r_{\text{ref}}$ (can be seen in term of geometrical optics)

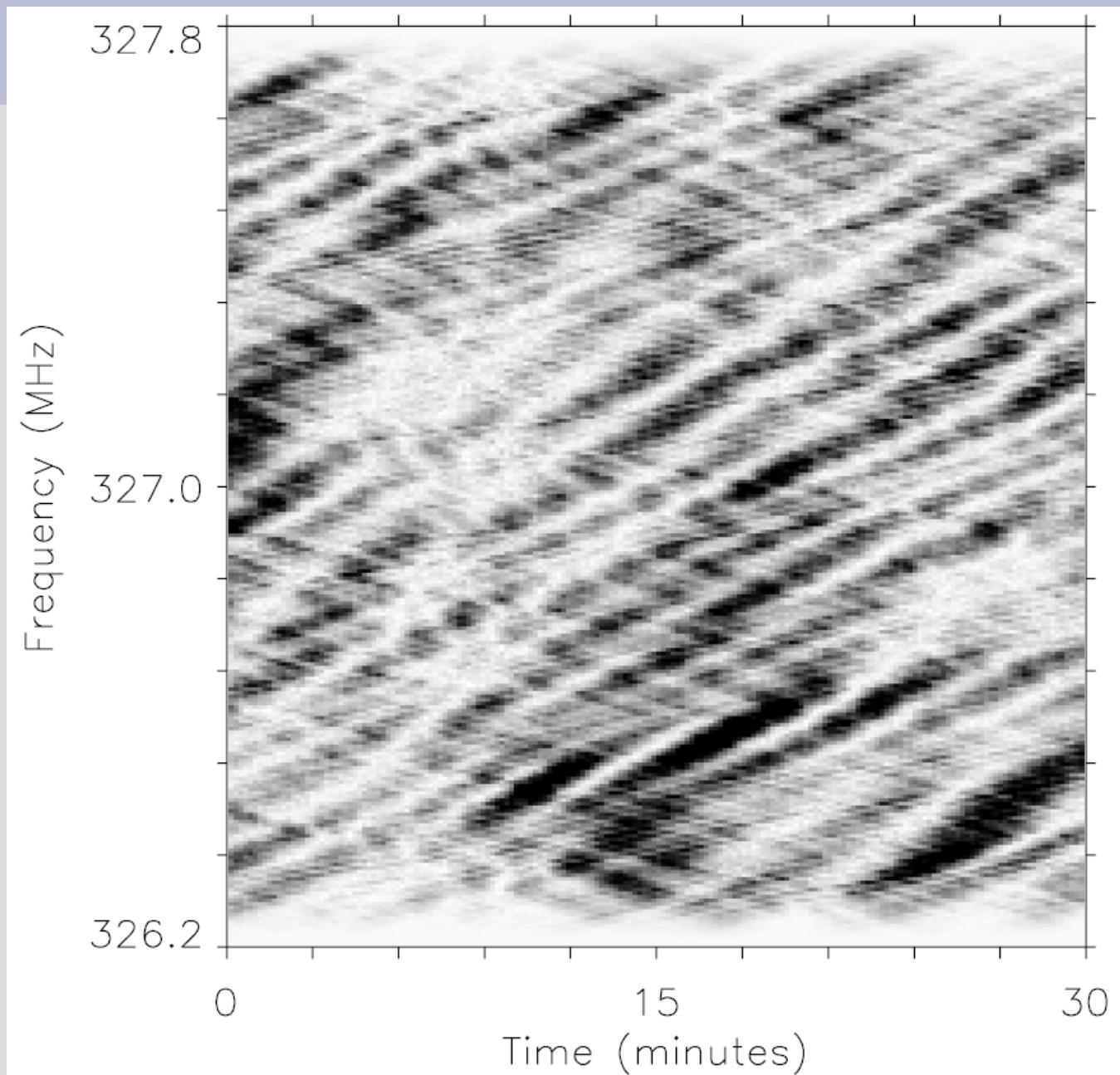
slow flux variations

modest limits on angular size :

many compact sources shown refractive scintillation

diffractive scintillation

Dynamic spectra on
pulsar B0834+06
at Arecibo
2003 Dec 31



Dispersion induced by the ionized Interstellar Medium

The ISM is a **cold and ionised plasma** :

frequency-dependent **index of refraction**

$$\mu = \sqrt{\left(1 - \left(\frac{f_p}{f}\right)^2\right)} , \quad v_g = \mu c$$

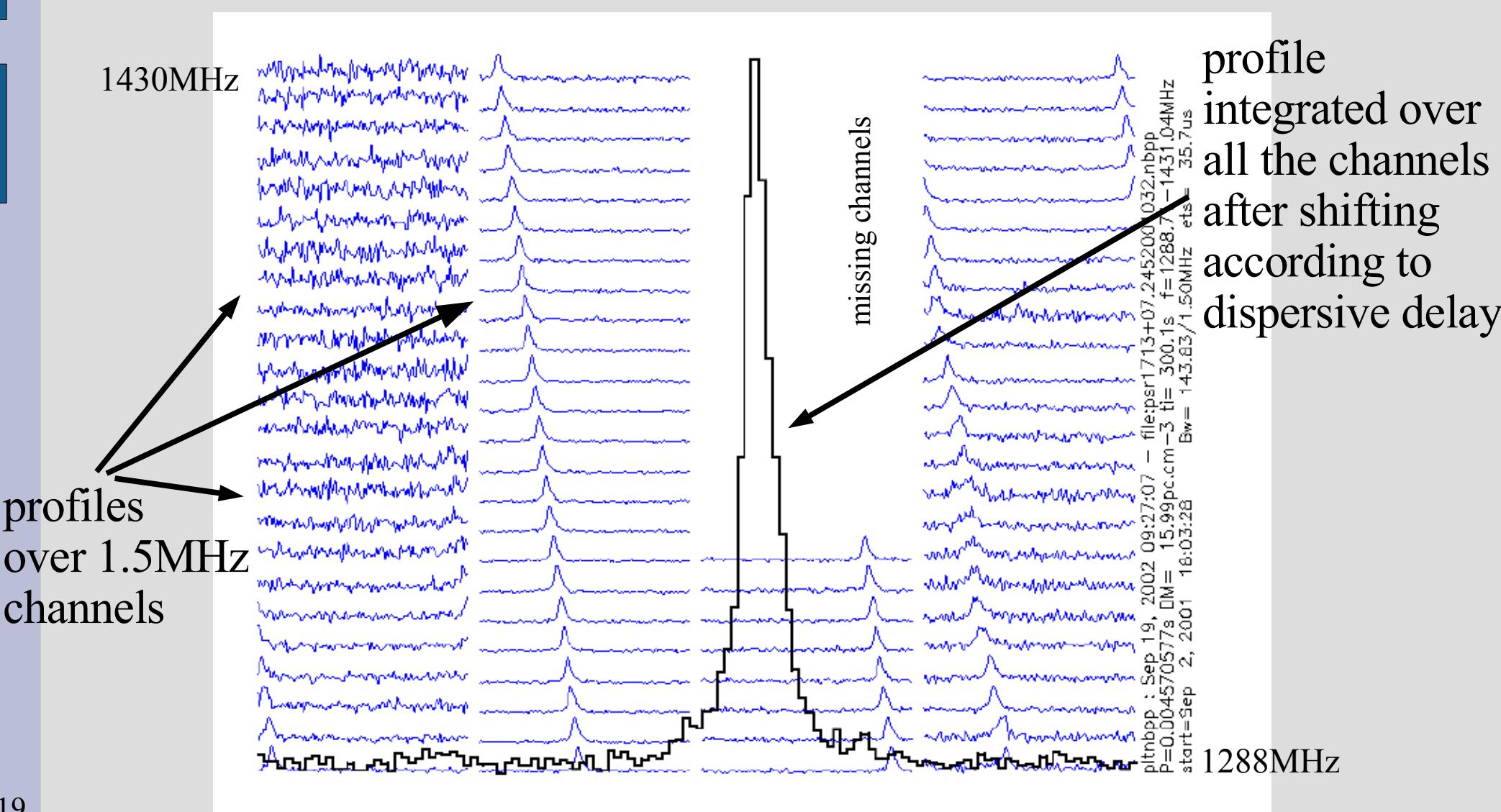
where f is the observing radio and f_p the plasma frequency

$$f_p = \sqrt{\frac{e^2 n_e}{\pi m_e}} \quad f_p \sim 1.5 \text{kHz} \text{ with } n_e \sim 0.03 \text{ cm}^{-3}$$

temporal delay with respect to infinite frequency :

$$t = \int_0^d \frac{dl}{v_g} - \frac{d}{c} \equiv D \frac{DM}{f^2} , \quad D \equiv \frac{e^2}{2 \pi m_e c} = 4148.808 \text{ Hz}^2 \text{ pc}^{-1} \text{ cm}^3 \text{ s}$$

Observation of pulsar PSR B1713+07 with NBPP showing dispersion and scintillation on Sep19,2002



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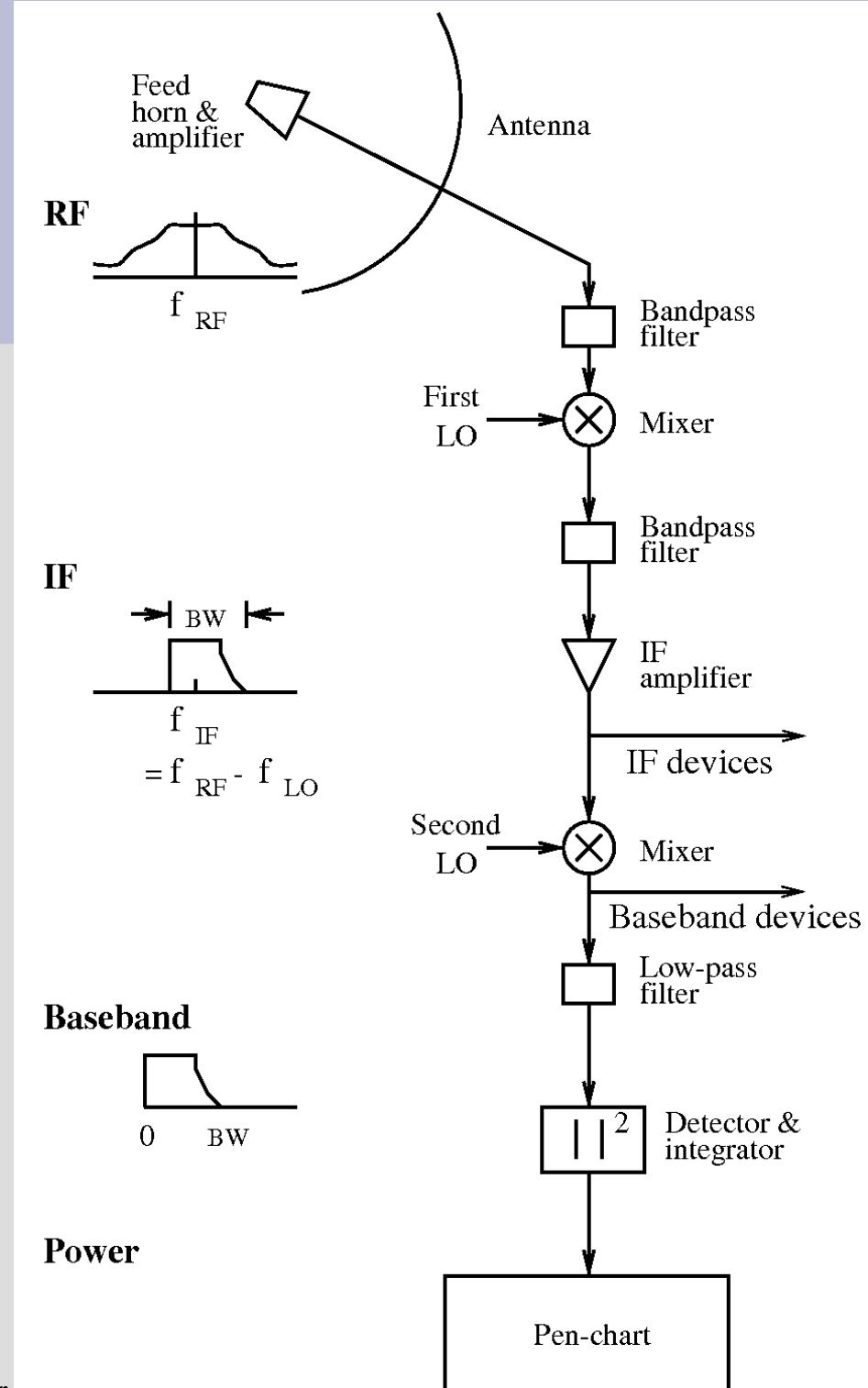
signal path in a radiotelescope

bandpass filter + mixer

IF amplifier to IF devices

mixer to baseband devices

low-pass filter
to detection and integration
pen-chart

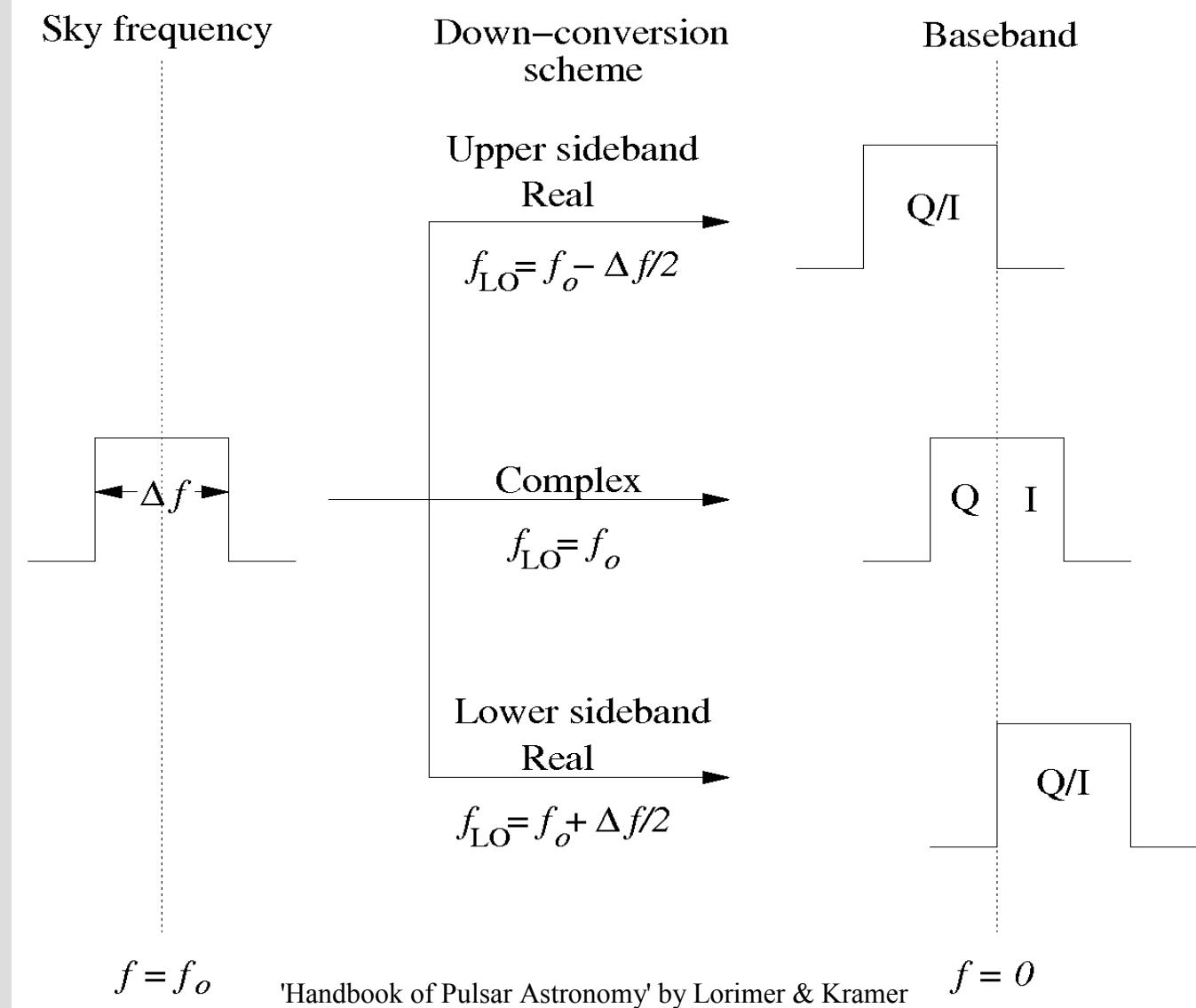


baseband mixing

mixing can be done
in several ways

a single LO at one end
of the passband
($f_o - \Delta f/2$ or $f_o + \Delta f/2$)
real sampled data
rate $2\Delta f$

a pair of LOs
in phase-quadrature
at the middle f_o
complex sampled data
rate Δf twice



ISM Transfer Function

delay in the ISM can be represented as
phase rotations depending on frequency and path length

$$\Delta \Psi = -k(f_o + f)d \quad , \quad k(f) = \frac{2\pi}{c} \mu f$$

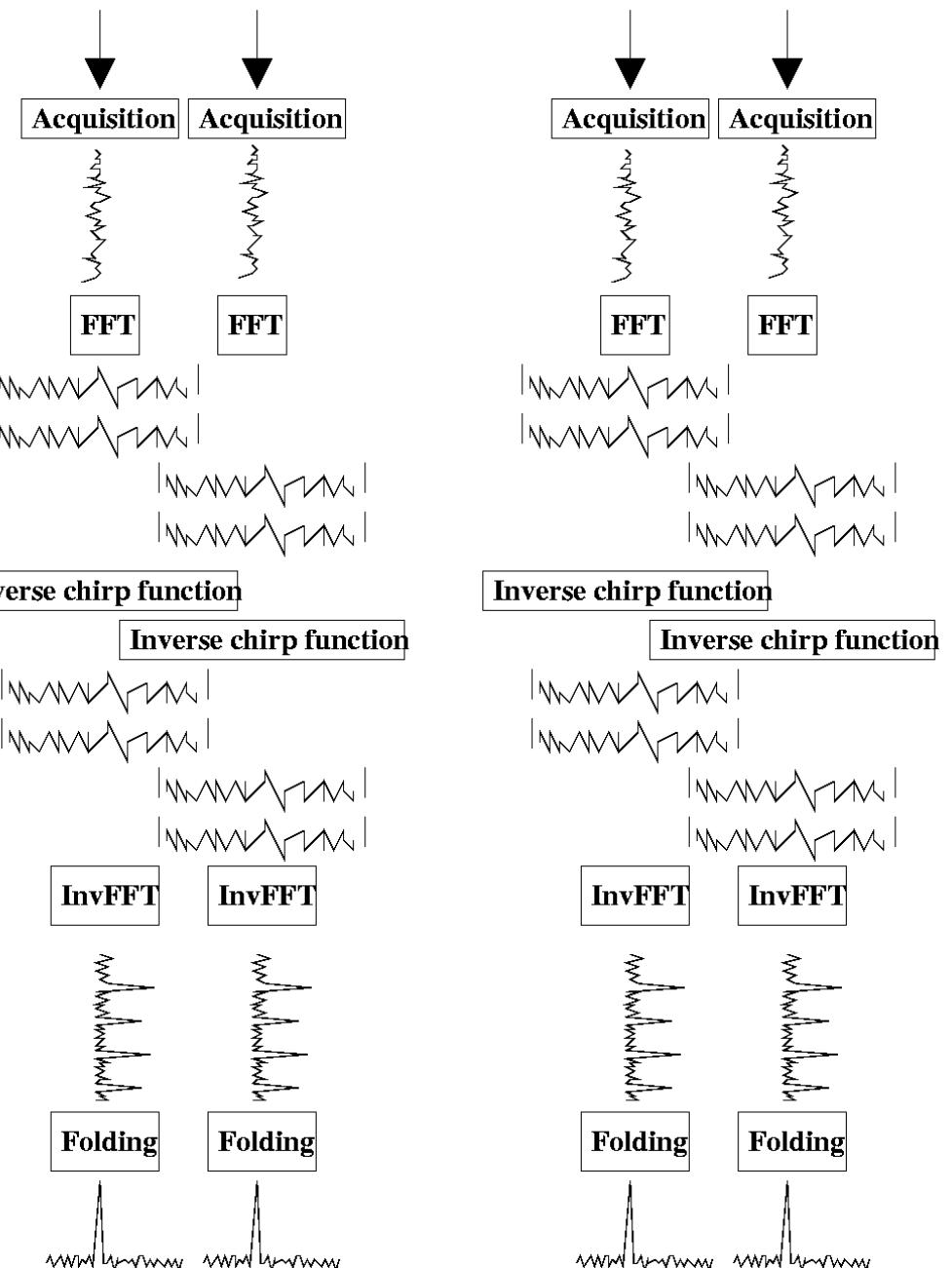
where k is the wave number
the transfer function is

$$H(f_o + f) = e^{-ik(f_o + f)d} \equiv e^{+i \frac{2\pi D}{(f + f_o)f_o^2} DM f^2}$$

dedispersion

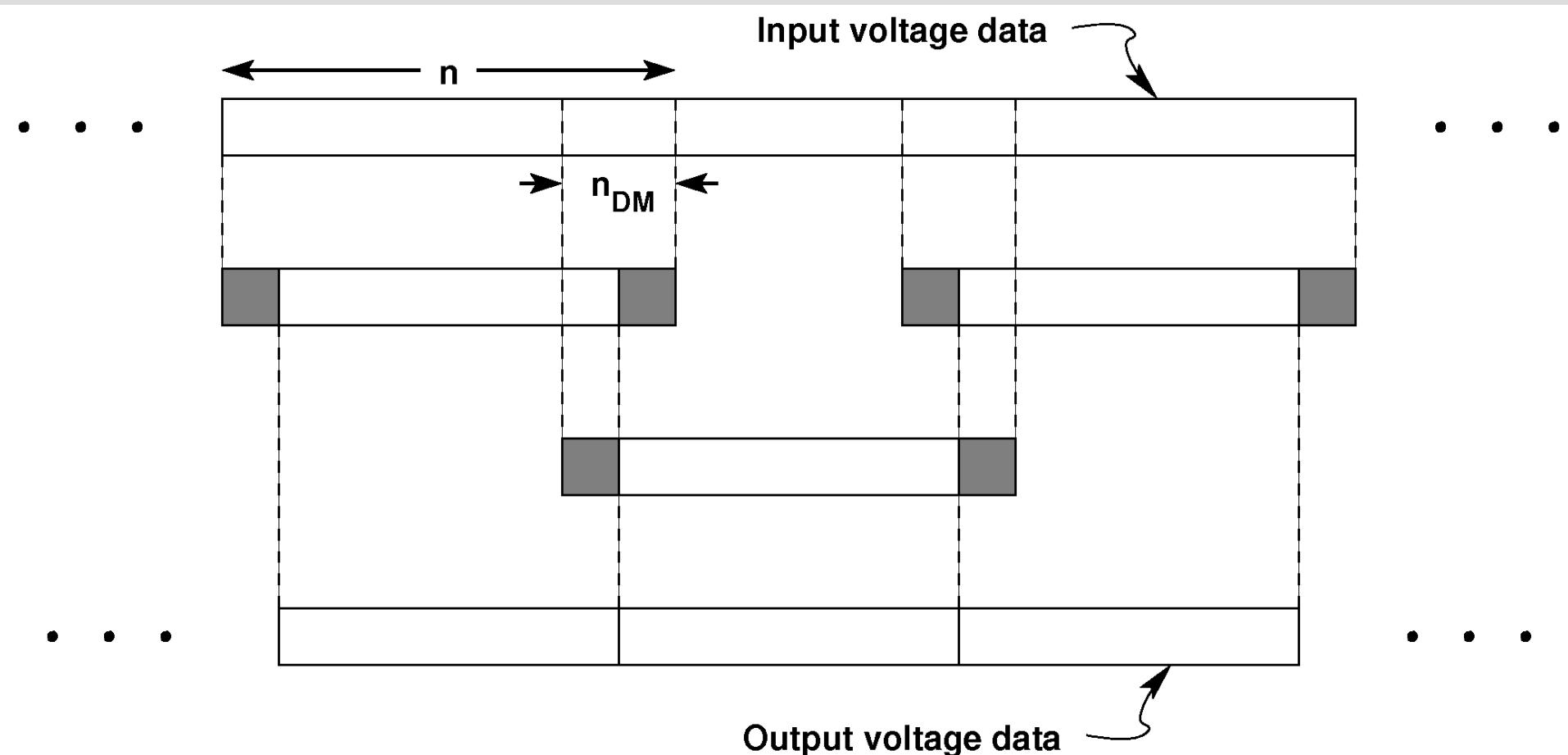
- a forward FFT
- multiplication by the inverse ISM transfer function
- a backward FFT
- folding coherently with varying pulsar period

2 complex polarizations



dedispersion : overlap

n_{DM} is the number of samples over which the radio profile is dispersed



Two kind of pulsar instrumentation

incoherent dedispersion

done after detection

on averaged intensity

à la durée du cycle de l'onde reçue

filterbank instrumentation

coherent dedispersion

done before detection

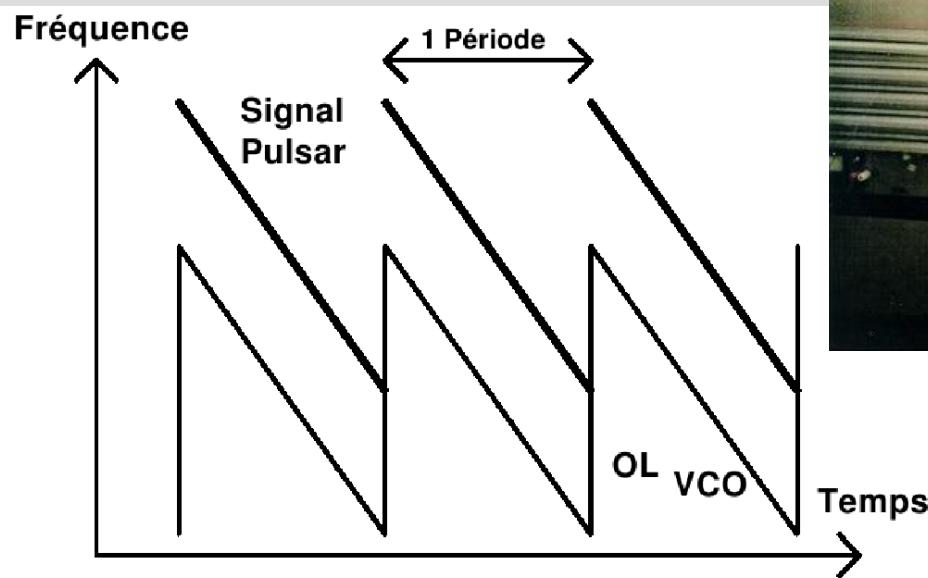
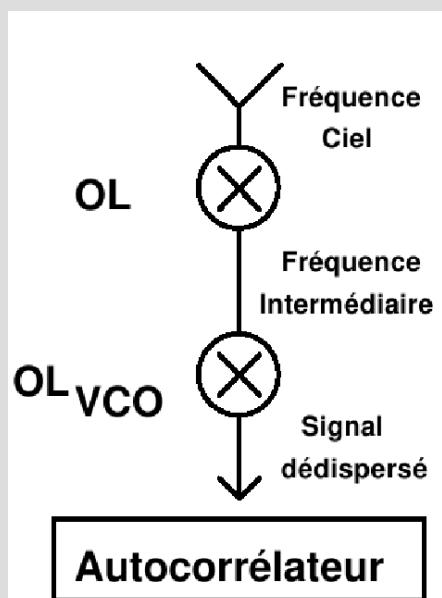
on voltages proportional to the received electric field,

before any integration, signal phase is preserved

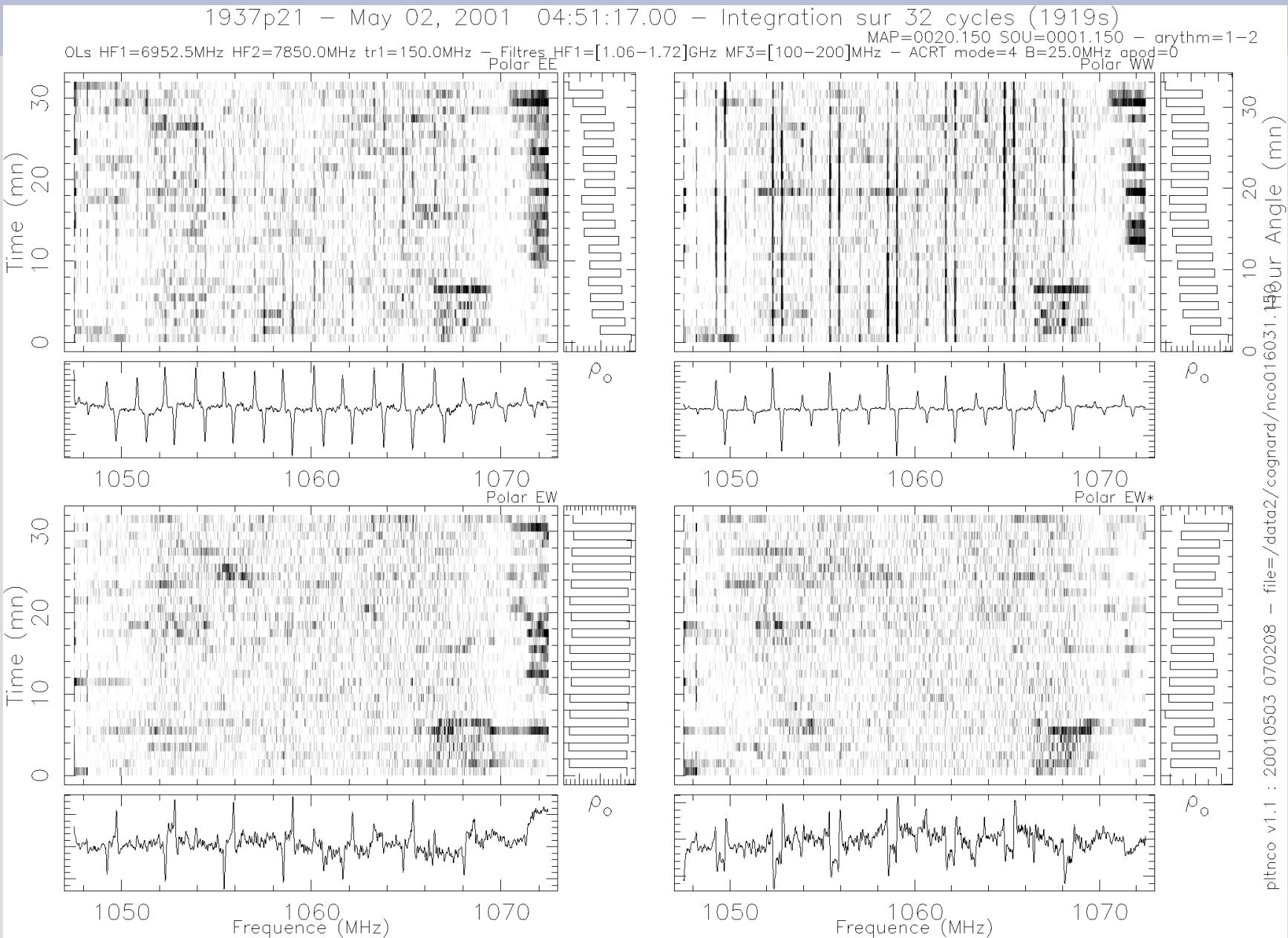
complex sampled baseband instrumentatsion or swept LO

the swept LO : a special coherent instrumentation

mixing of sky signal with a swept LO emulating
the effect of the ionized ISM
analyzing the output with a standard spectrometer

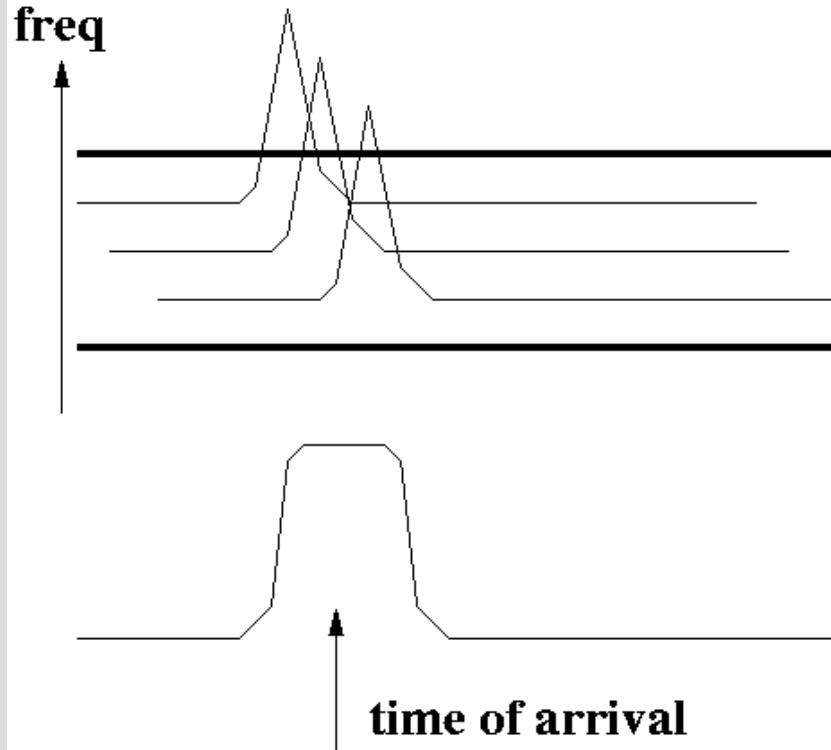


PSR B1937+21 swept LO observation



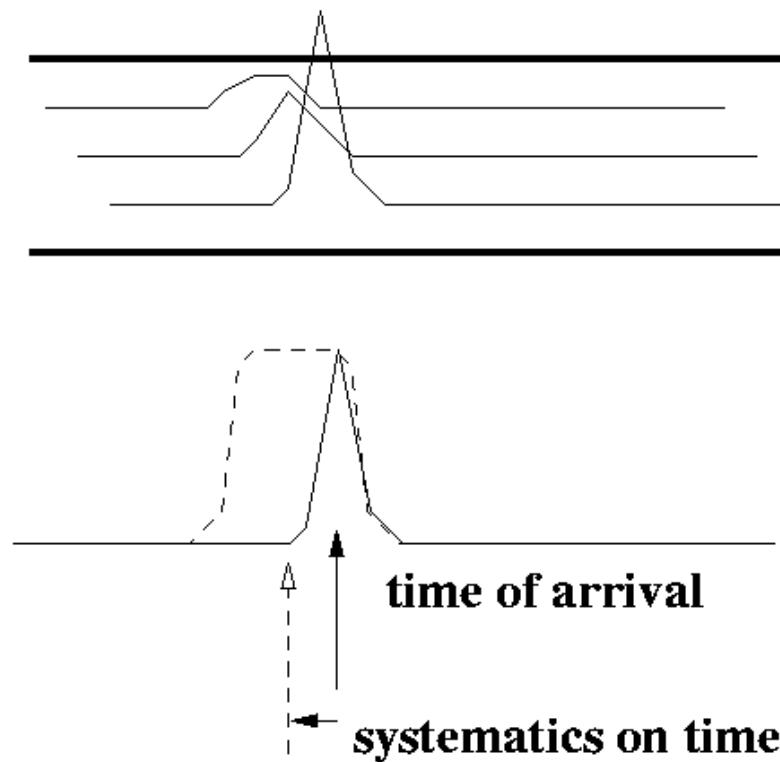
For filterbank instrumentations,
together with scintillation, the residual dispersion within channels
provide systematics on times of arrival...

NO SCINTILLATION



SCINTILLATION

pulsar is only partly present
in the channel bandwidth



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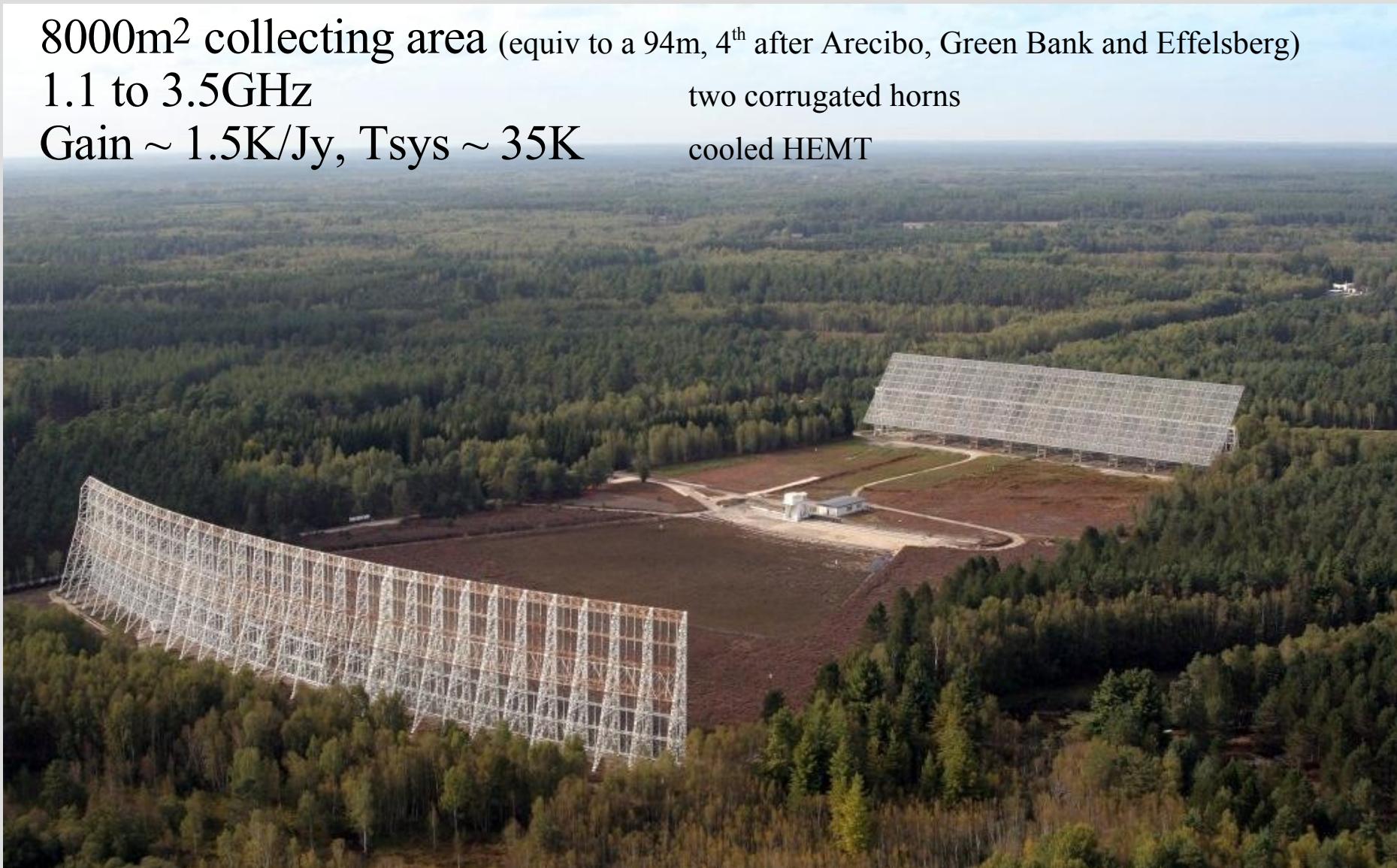
- Examples

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Nançay radiotelescope

8000m² collecting area (equiv to a 94m, 4th after Arecibo, Green Bank and Effelsberg)
1.1 to 3.5GHz
Gain ~ 1.5K/Jy, Tsys ~ 35K

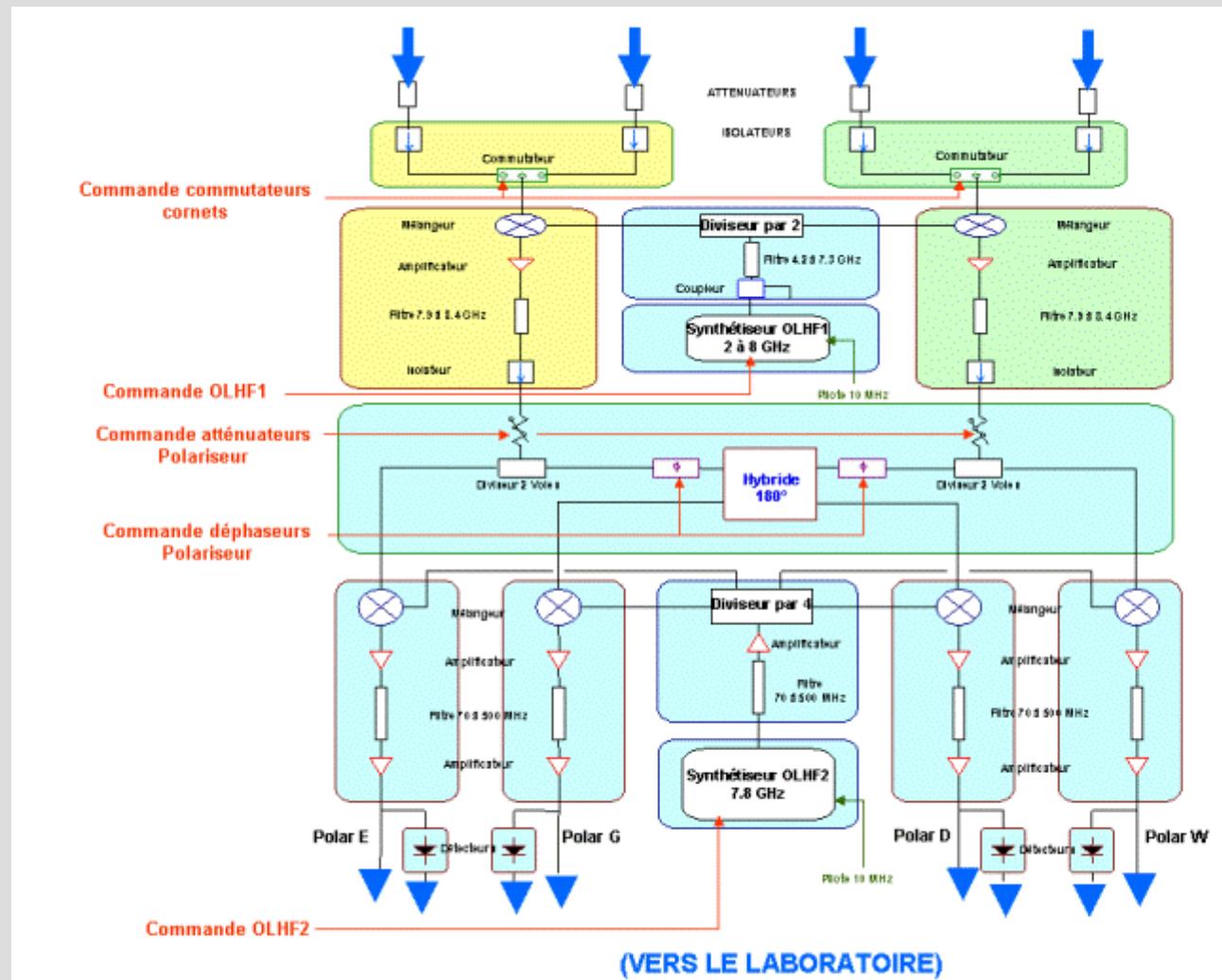
two corrugated horns
cooled HEMT



Nançay radiotelescope

data path

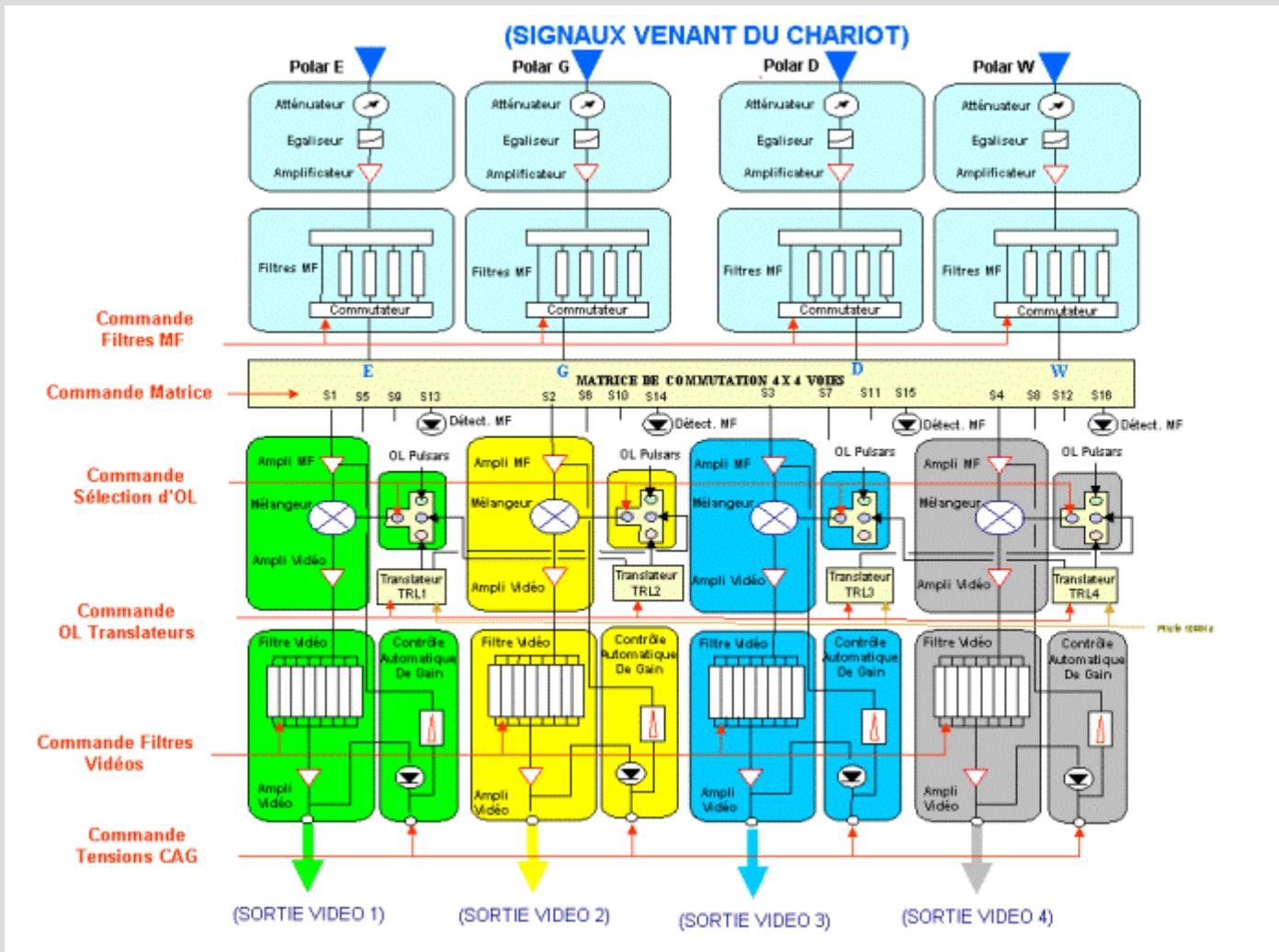
full coverage from 1.1 to 3.5GHz



Nançay radiotelescope

data path

400MHz instantaneous bandwidth

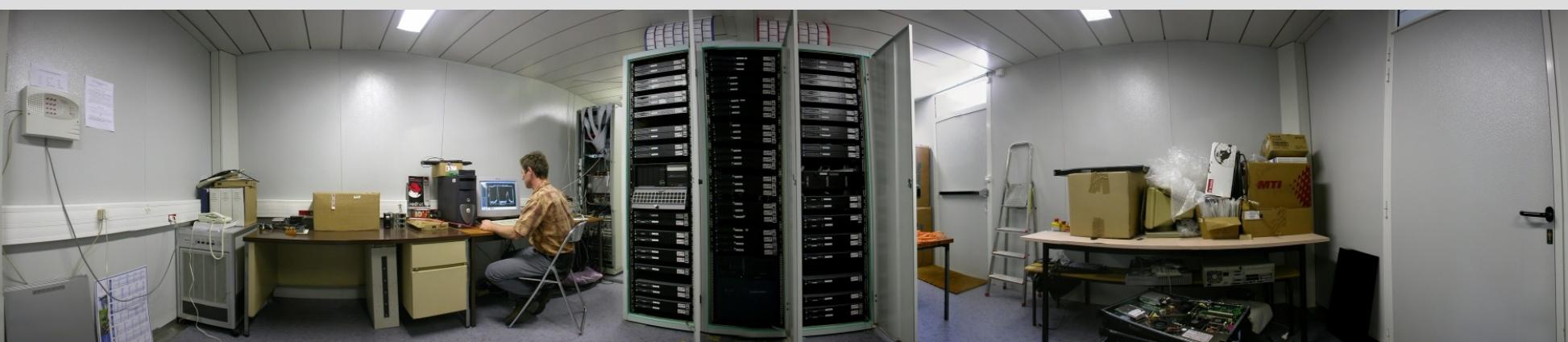




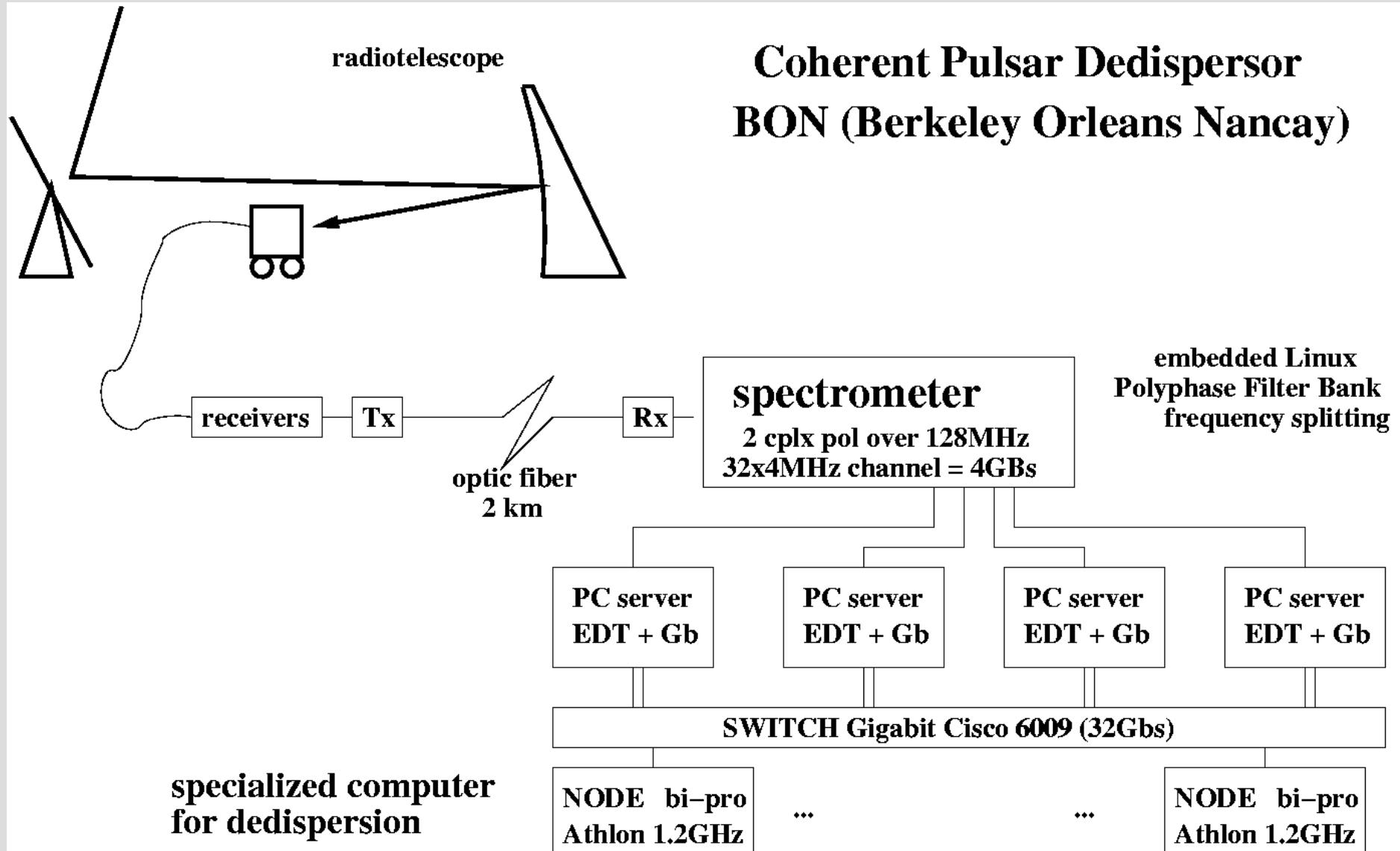
Pulsaroscope 1988-...
swept oscillator



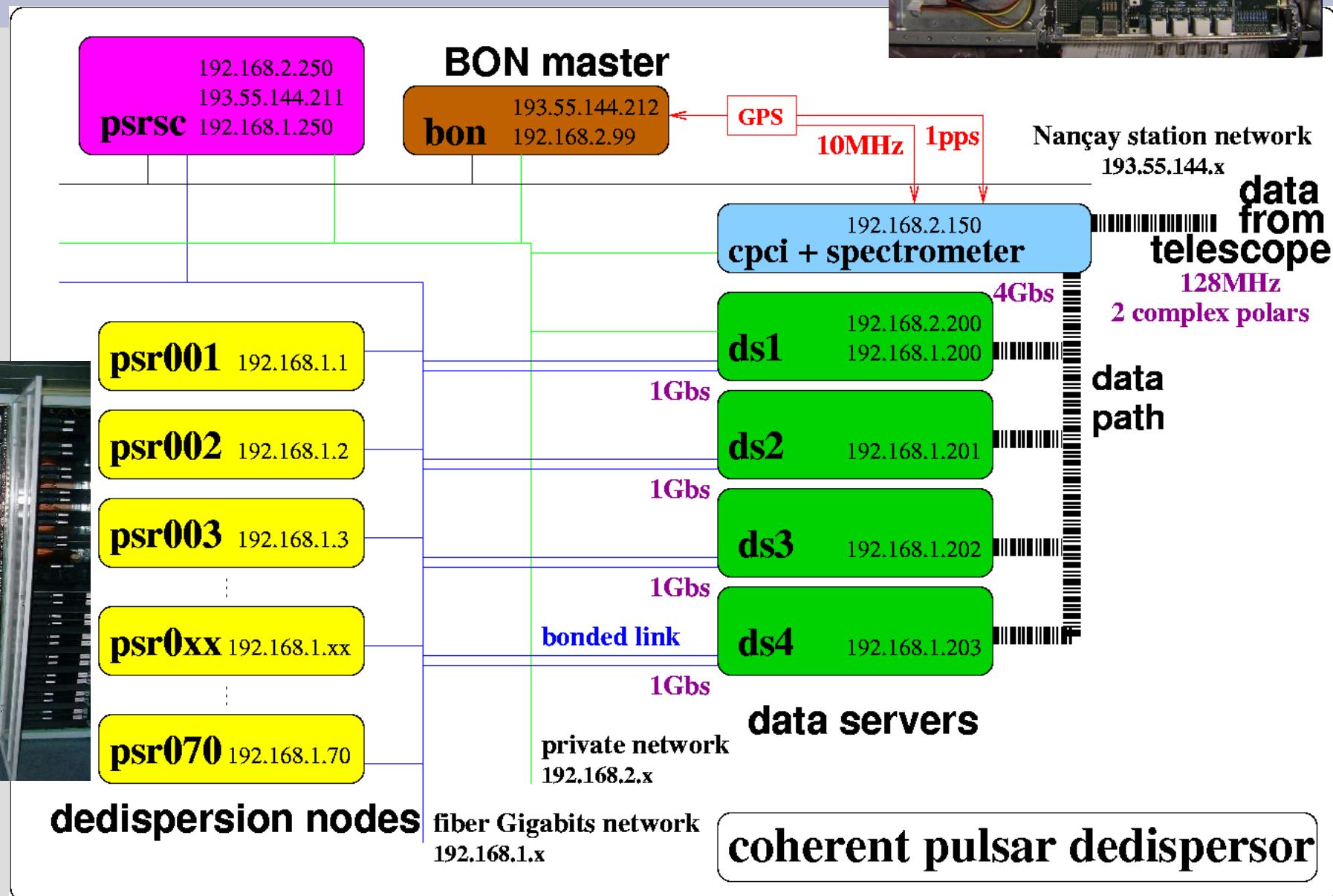
NBPP 1998-2003
(Navy Berkeley Pulsar Processor)



BON : the coherent pulsar dedispersor at Nançay



BON : the coherent pulsar dedispensor at Nançay



Serendip V

2 polars I,Q
sampled at 128Ms/s, 8bits
PFB : 32 4MHz channels
+
CPV5350 Motorola
embedded Linux

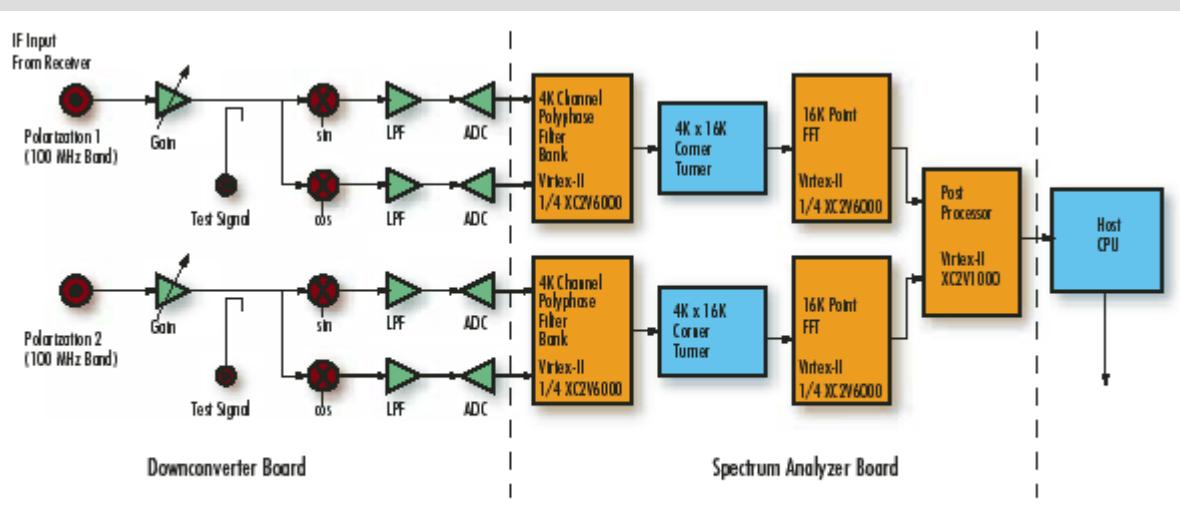
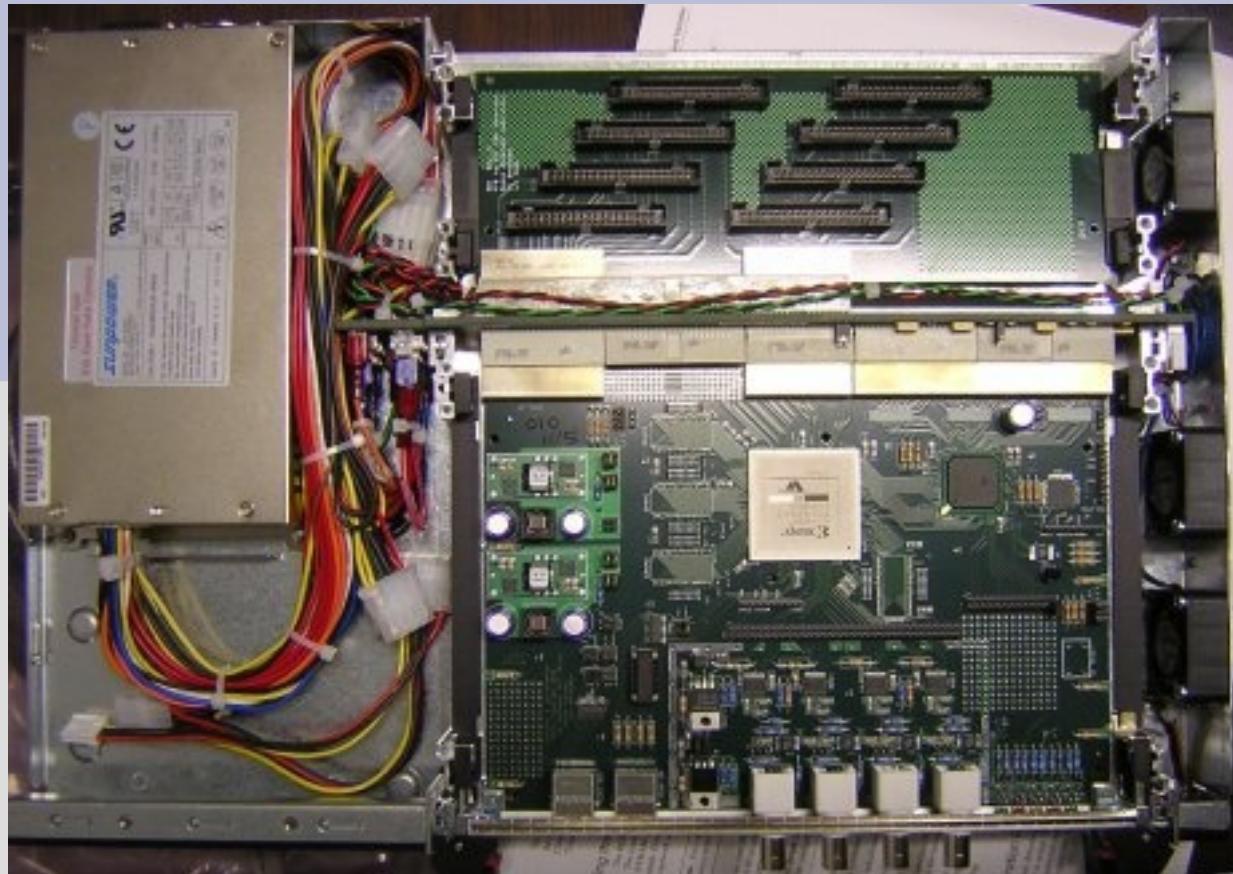
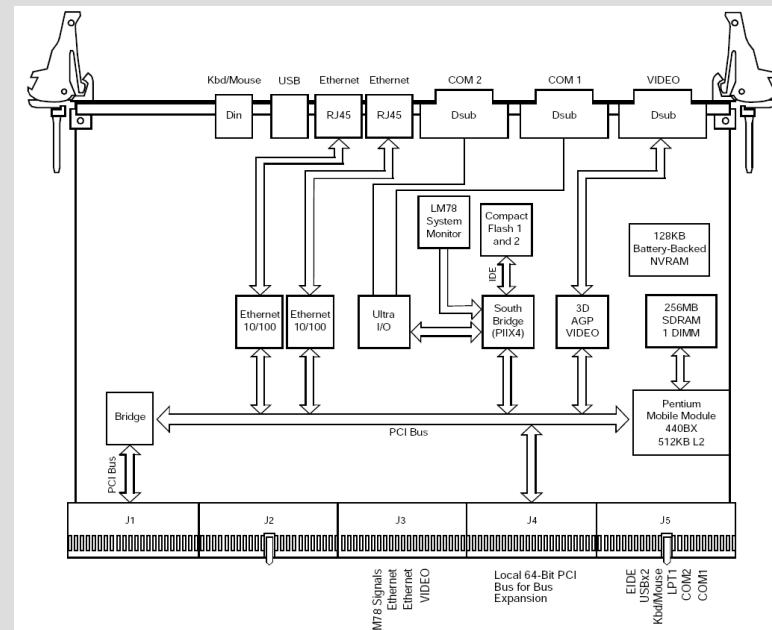


Figure 3 – SERENDIP V spectrometer module

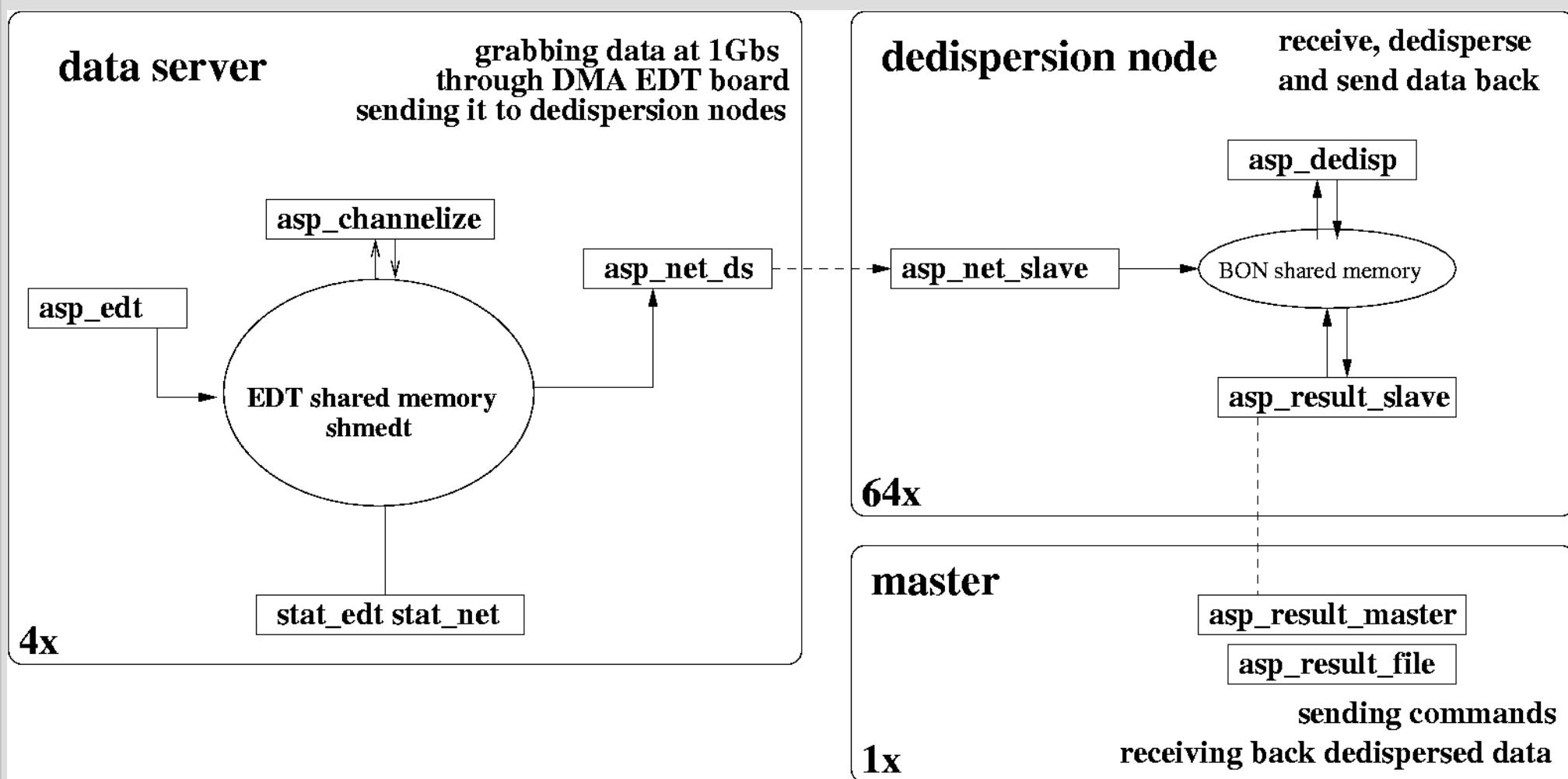


A dedicated calculator for BON



1 master bi-processor Athlon
1.2GHz, 2Go memory
77 slaves bi-proc Athlon 1.2GHz,
1 Go memory, 10G hard disk
Gigabit network (32GBs)
switch Cisco 6009
operating system
Linux, kernel 2.4.2 "optimized"

C real-time code



a precise datation 1/3

Clock and Data sent by Serendip V to dataservers
starts on the leading edge
of a 1pps signal (pps = pulse per second)

1pps signal and 10MHz reference clock
are provided by a GPS disciplined clock



Thunderbolt GPS disciplined clock,
Trimble Inc.

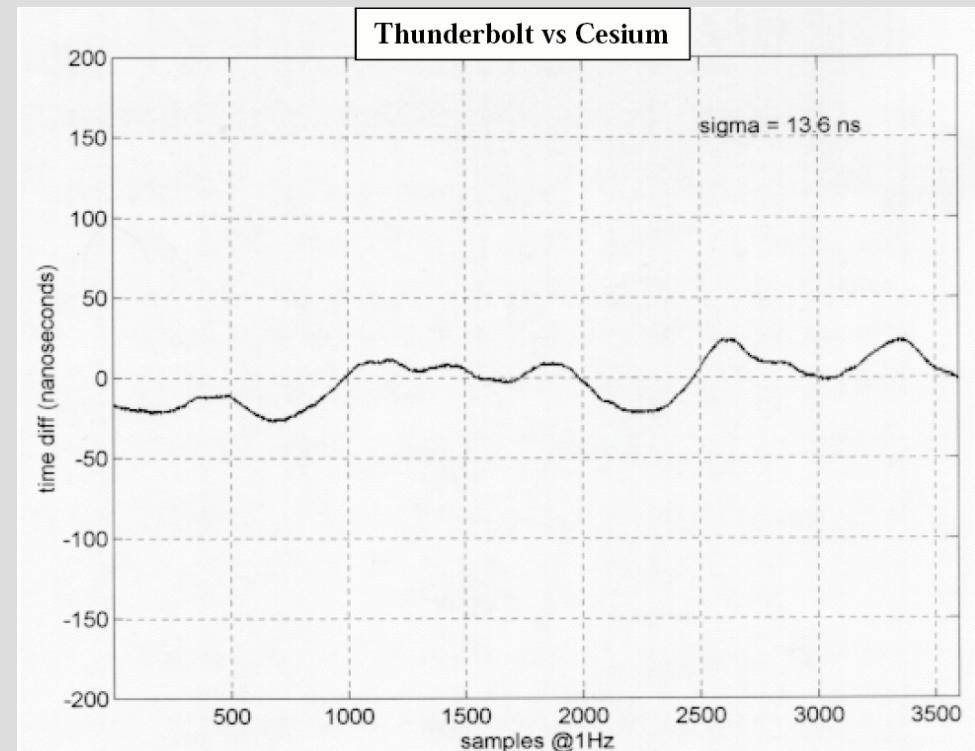
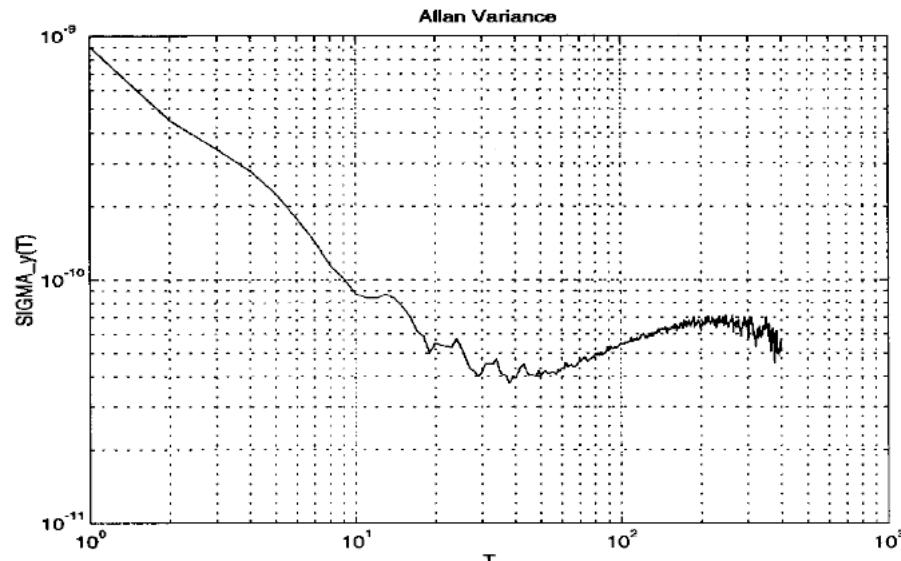


a precise datation 2/3

Thunderbolt GPS Disciplined Clock *GPS Clock for the Wireless Infrastructure*

PERFORMANCE SPECIFICATIONS

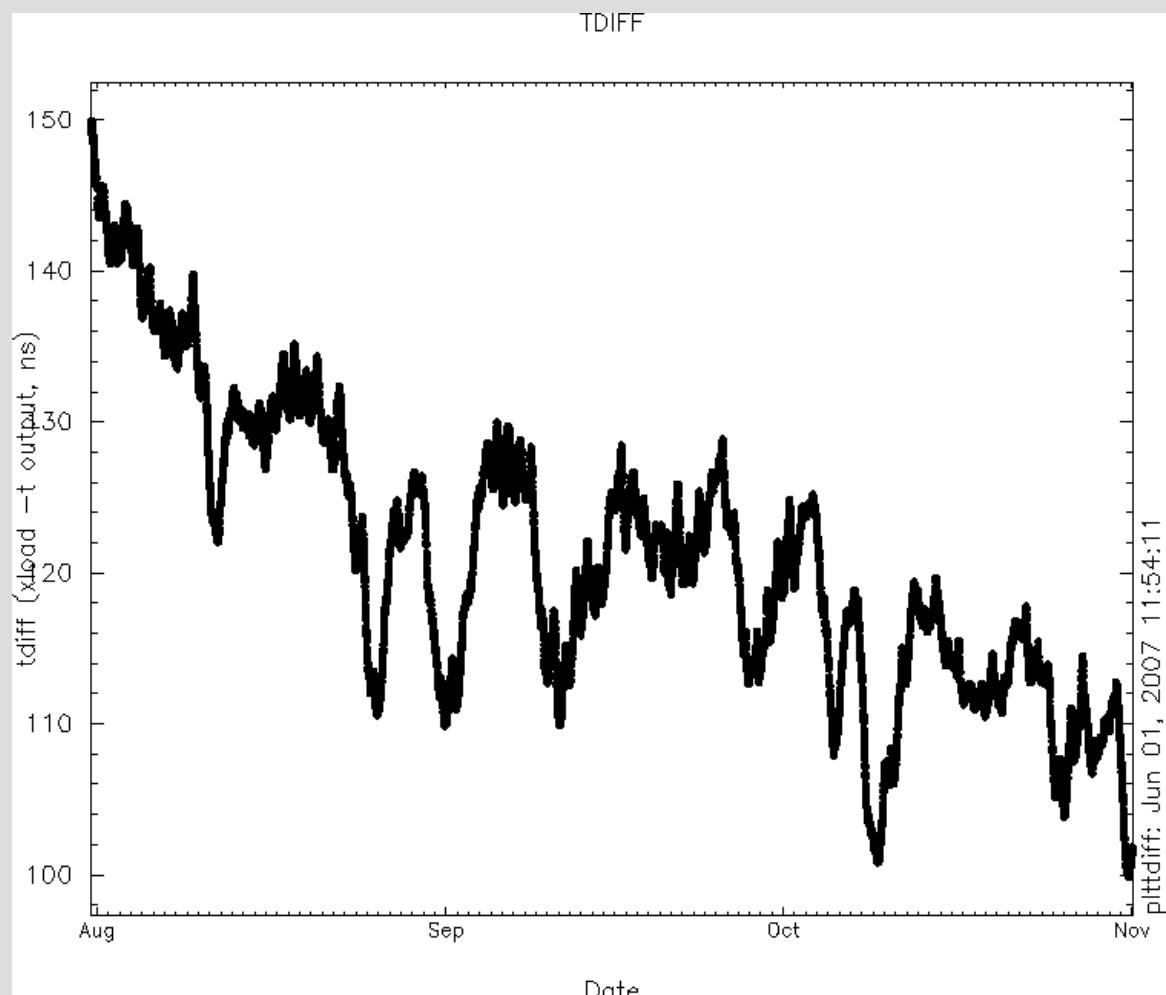
General	L1 frequency, CA/code (SPS), 8-channel continuous tracking receiver
Update rate	1 Hz
PPS accuracy	UTC 20 nanoseconds (one sigma)
10 MHz accuracy	1.16×10^{-12} (one day average)
10 MHz stability	See graph below



Comparison with a Cesium
Specifications

a precise datation 3/3

time difference (in ns) between
1pps signal and
the leading edge
of SerendipV internal clock



A running observation...

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Timing of pulsars

determine the arrival times
of radio pulses received on Earth

this needs

- a precise reference clock
- a special instrumentation
 - to integrate the signal
in time and frequency

analyze the shape of the time of arrival residuals

Détermination of Times of Arrival (TOA)

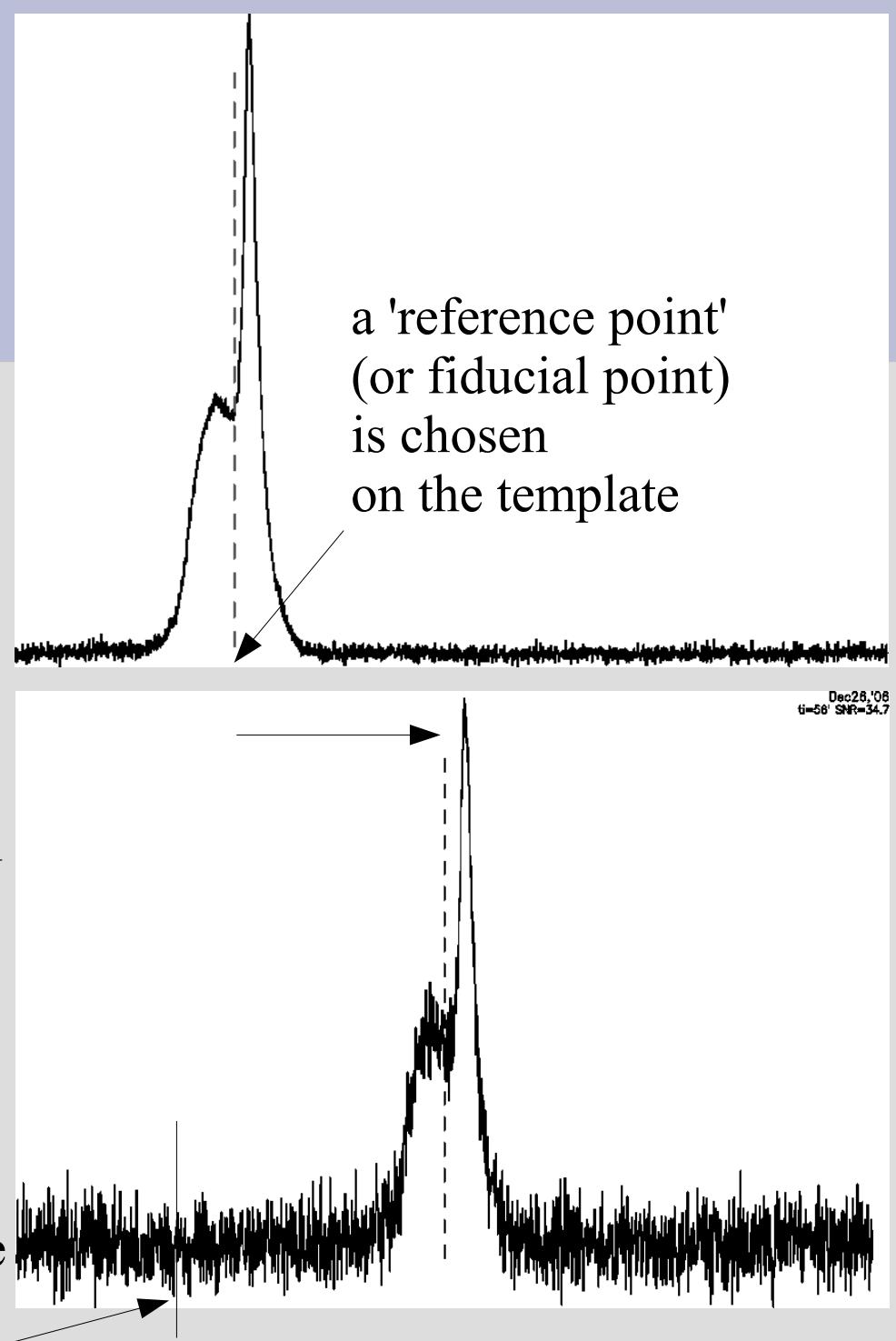
(example on PSR J1600-3053 P=3.6ms, binary)

build a '**template**', either

- smoothed version
of a given observation
- sum of sinus/cosinus
- coherent integration
of many observations

cross-correlation of the '**template**' with
the daily observation yields
a shift converted to a time of arrival

position of the first data sample
corresponding to the start time
will be taken into account



Times of Arrival for J1600-3053

f	1	1600-30	1368.000	54033.5511921591647	0.48
f	1	1600-30	1368.000	54036.5385764225914	0.54
f	1	1600-30	1368.000	54048.5021991052575	0.59
f	1	1600-30	1368.000	54051.5056597667359	0.50
f	1	1600-30	1368.000	54054.4968287444377	0.46
f	1	1600-30	1368.000	54056.4913888998682	0.48
f	1	1600-30	1368.000	54057.4889815273292	0.52
f	1	1600-30	1368.000	54060.4810301095328	0.51
f	1	1600-30	1368.000	54065.4600579101507	0.60
f	1	1600-30	1368.000	54071.4479745723167	0.57
f	1	1600-30	1368.000	54072.4445486474761	0.53
f	1	1600-30	1368.000	54079.4312384526258	0.50

observatory_code, '1', pulsar_name, radio_frequency[MHz], TOA[MJD], uncertainty[μs]

Analysis of Times of Arrival

minimize the differences

MEASURED TOAs – CALCULATED TOAs

this can be done with different codes :

- tempo (Princeton, then Parkes)
- antiope (Meudon, then Orléans)
- timapr (O.Doroshenko)

tempo

input files : parameters + TOAs

1600.par :	PSRJ	J1600-3053	
	RAJ	16:00:51.90392	0
	DECJ	-30:53:49.325	0
	DM	52.333	
	PEPOCH	52500.0	
	F0	277.937711457601	1
	F1	-7.322E-16	1
	PMRA	-0.91	
	PMDEC	-4.0	
	POSEPOCH	52500.00	
	EPHEM	DE405	
	BINARY	DD	
	PB	14.348457554	1
	E	0.00017371	1
	A1	8.8016571	1
	T0	52506.3711244	1
	OM	181.768043	1

tempo

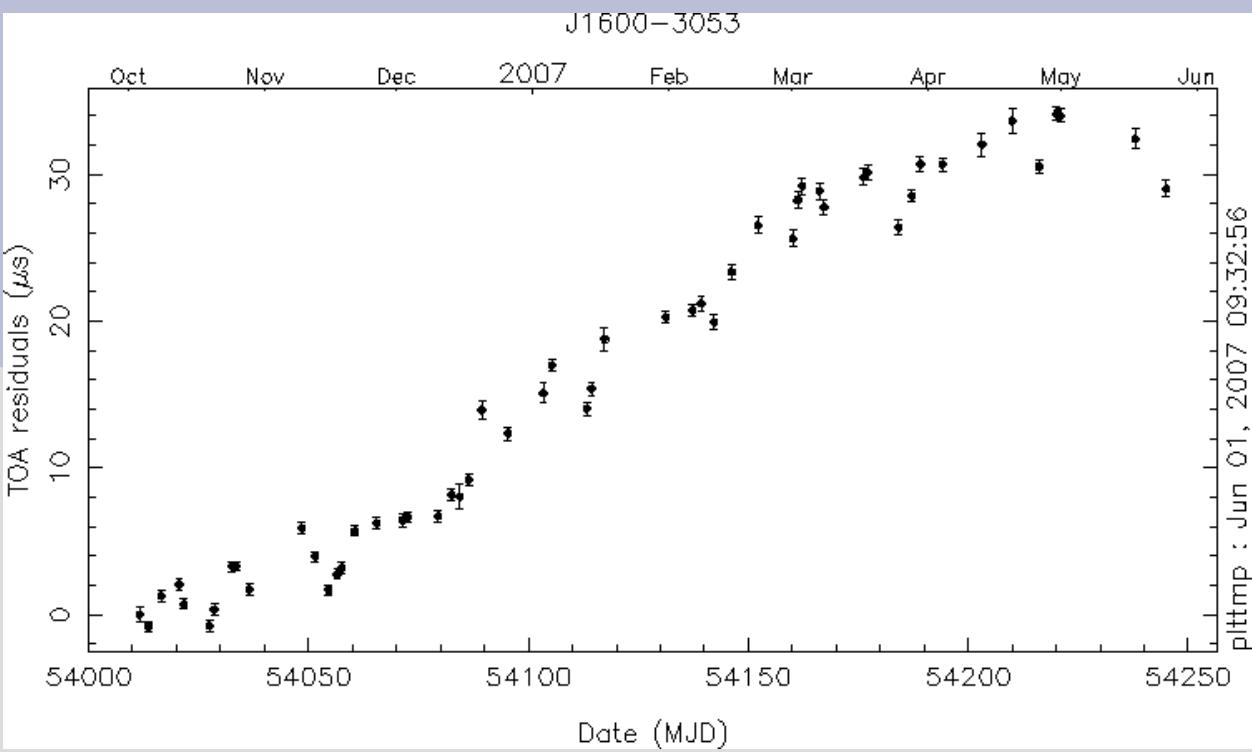
output file is tempo.lis

PSR J1600-3053 Ephem: DE405 Clk: UNCORR				P	Ref:	52500.0000	Pos	Ref:	52500.00	
	RA	DEC		PM	RA	PM	DEC	PM	RV	PARALLAX
16 00 51.90392002	-30 53 49.3250000			-0.9100		-4.0000		0.0000		0.0000
0.00000000		0.00000000		0.0000		0.0000		0.0000		0.0000
0.00000000		0.00000000		0.0000		0.0000		0.0000		0.0000
16 00 51.90392002	-30 53 49.3250000			-0.9100		-4.0000		0.0000		0.0000
F0	F1 (D-15)			F2 (D-23)			F3 (D-00)			
277.93771145760098307	-0.732200000000			0.000000000			0.000000			
0.00000016961066173	-2.442771193969			1.751614040			0.000000			
0.00000001266097278	0.180663222978			0.128783973			0.000000			
277.93771162721162682	-3.174971193969			1.751614040			0.000000			
P0	P1 (D-15)			DM	DM1		PPN GAM			
0.0035979284522264215	0.000009478394			52.333000	0.000000		1.000000			
-0.000000000021956252	0.000031621891			0.000000	0.000000		0.000000			
0.000000000001638974	0.000002338702			0.000000	0.000000		0.000000			
0.0035979284500307963	0.000041100285			52.333000	0.000000		1.000000			
A1 sin(i)	E	T0 (MJD)		PB	OMEGA					
8.801657100	0.0001737100	52506.371124400		14.348457554000	181.768043					
-0.000000265	0.0000000798	-0.000883024		-0.000000022373	-0.022206					
0.000000178	0.0000000448	0.000576593		0.000000010718	0.014472					
8.801656835	0.0001737898	52506.370241376		14.348457531627	181.745837					
Mass function: 0.0035560316 +/- 0.000000002 solar masses										
Weighted RMS residual: pre-fit				11.887 us.	Predicted post-fit		0.835 us.			

tempo

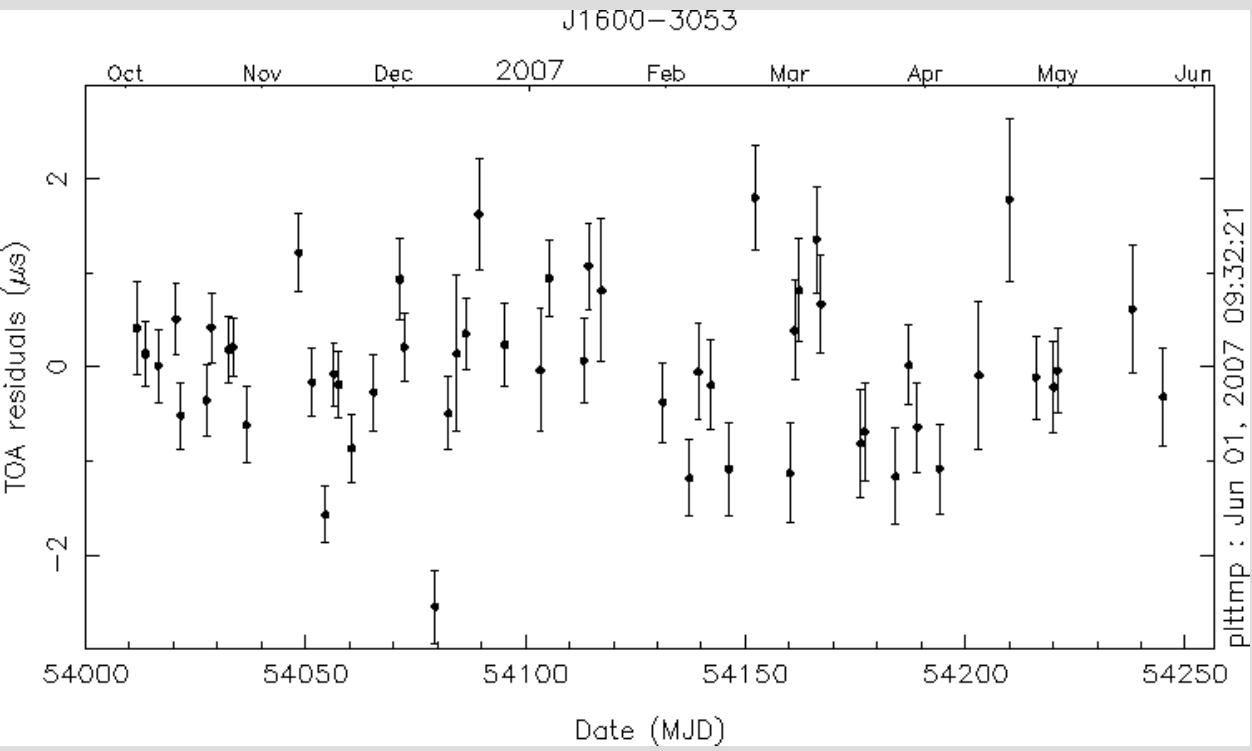
pre-fit

TOAs residuals
before adjustment of parameters



post-fit

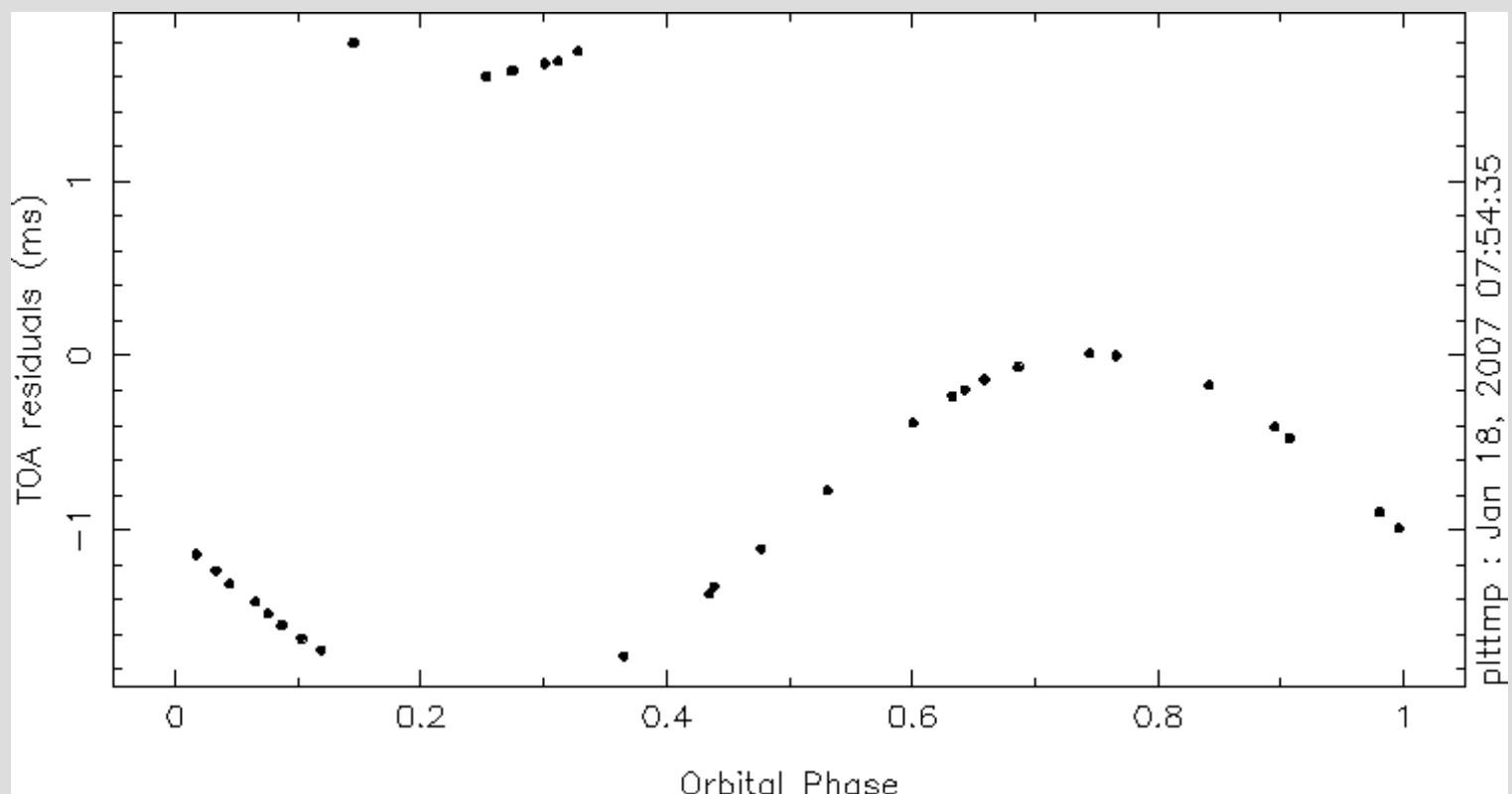
TOAs residuals
after adjustment of parameters



tempo

pre-fit

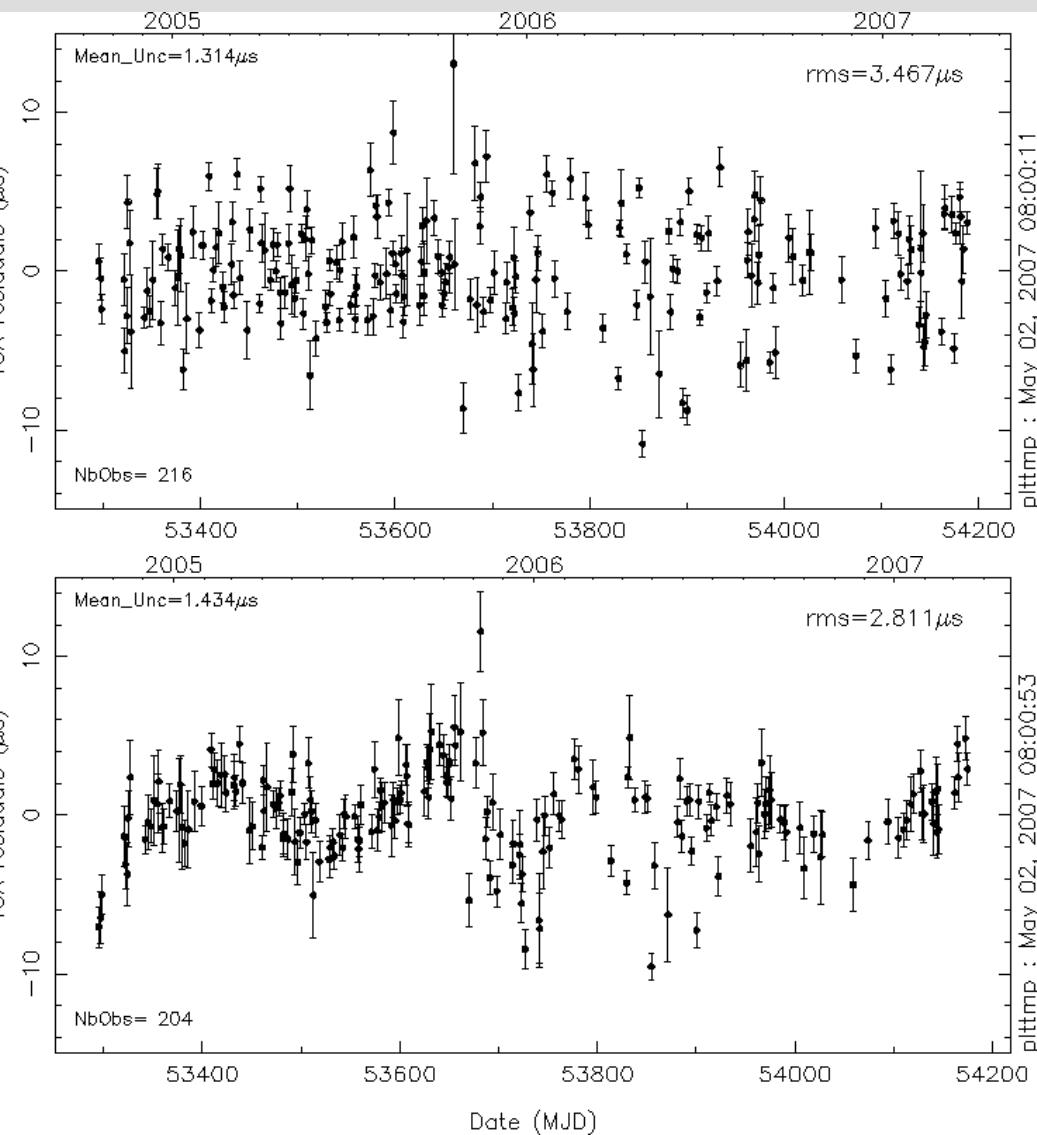
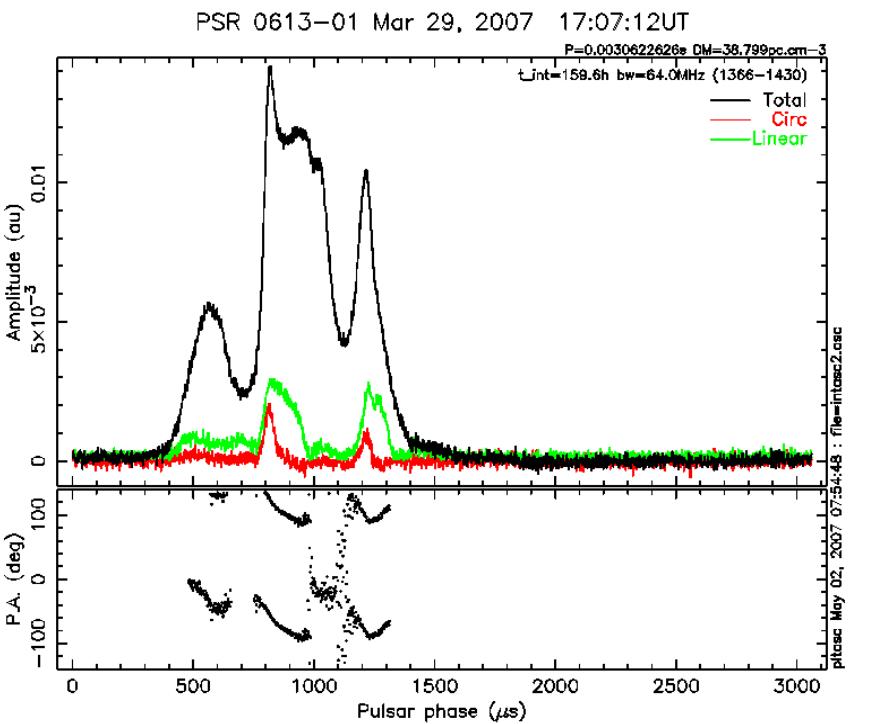
with a 10^{-4} relative offset on $A_1 \sin(i)$



PSR J0613-0200

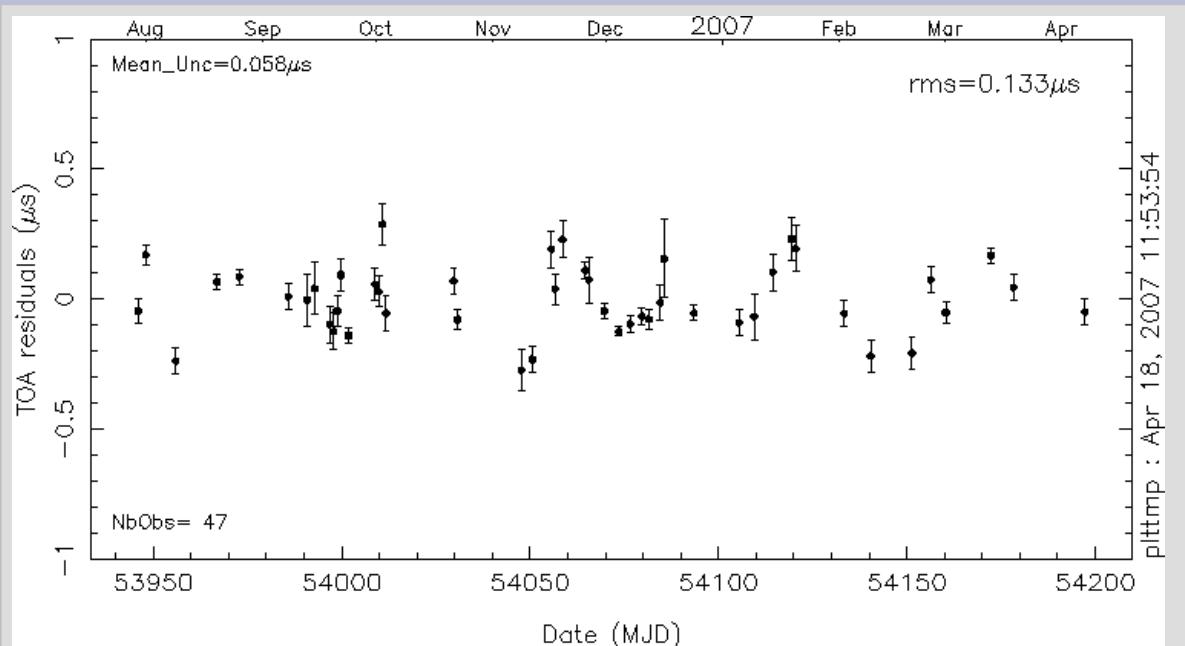
$P=3.062\text{ms}$ $P_{\text{Bin}}=1.2\text{days}$

Comparison between integrated daily profiles for observational parameters refined parameters

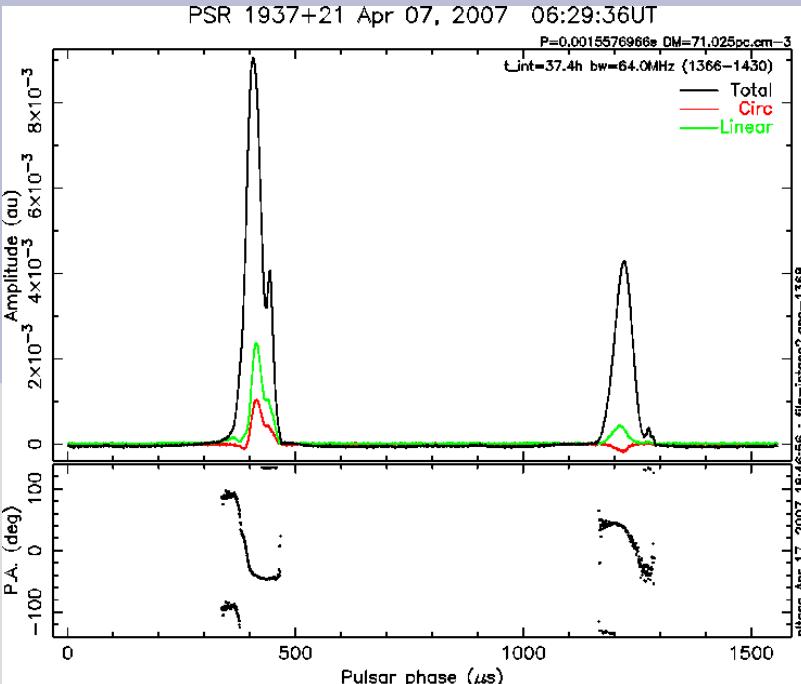


PSR B1937+21

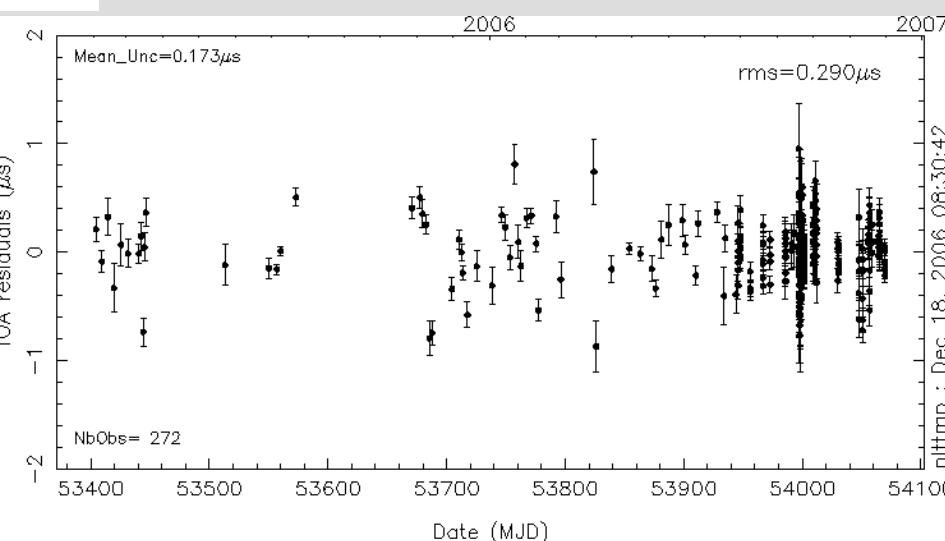
$P=1.557\text{ms}$ isolated



uncertainty 60ns over ~20mn
residuals rms 130ns



uncertainty 170ns over 30sec
residuals rms 290ns over ~2ans



Limiting factors

Multipath produces varying scattering tails, tiny changes in the shape of daily profiles yield to systematics in TOAs

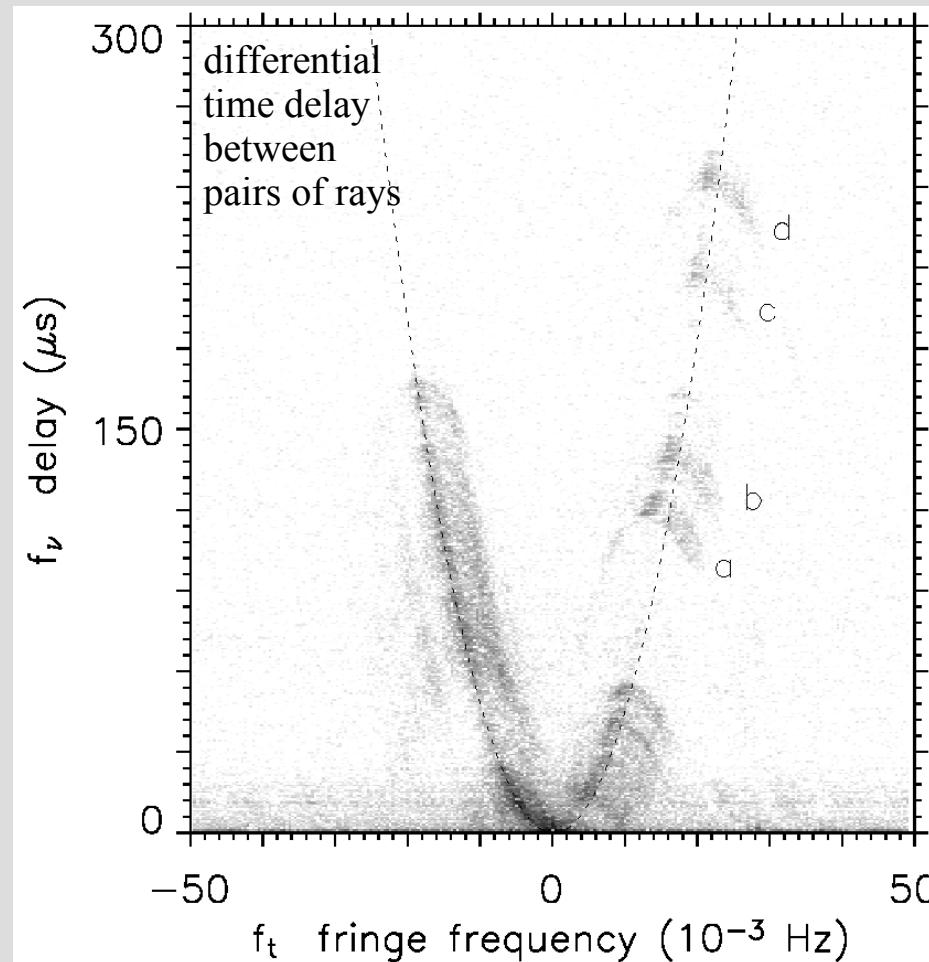
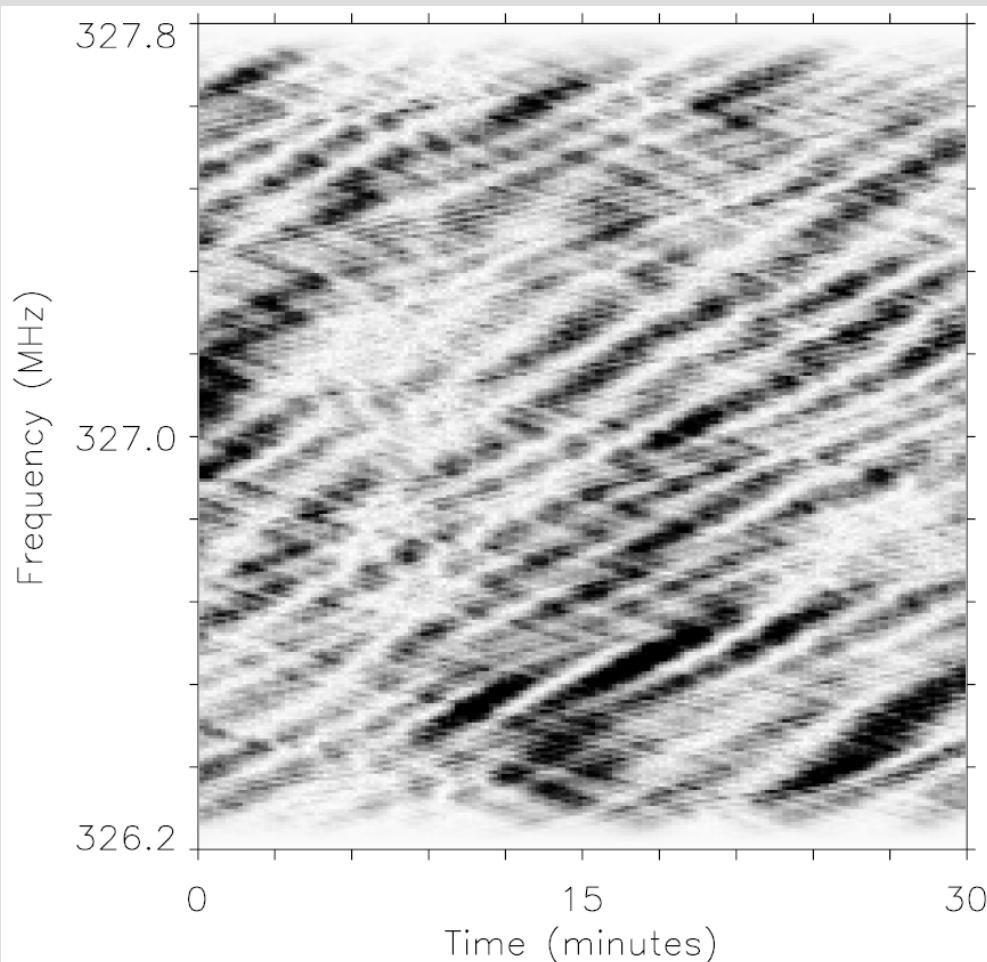
How much is the mean pulse affected by low level contribution of delayed pulses ?

Should we routinely produce a secondary spectrum to be able to correct TOAs ?

dynamic spectra

secondary spectra

squared modulus of
the Fourier transform of
the dynamic spectrum



Conclusion

a stable local clock
a baseband dedispersor
a large telescope

and high quality timing measurements of millisecond pulsars
are achieved...

and metrology in radioastronomy becomes a reality !